

Numerical Calculation of Solid-Liquid two-Phase Flow Inside a Small Sewage Pump

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ABSTRACT

Based on a mixture multiphase flow model, the RNG k - ϵ turbulence model and frozen rotor method were used to perform a numerical simulation of steady flow in the internal flow field of a sewage pump that transports solid and liquid phase flows. Results of the study indicate that the degree of wear on the front and the back of the blade suction surface from different densities of solid particles shows a completely opposite influencing trend. With the increase of delivered solid-phase density, the isobaric equilibrium position moves to the leading edge point of the blade, but the solid-phase isoconcentration point on the blade pressure surface and suction surface basically remains unchanged. The difference between hydraulic lift and water lift in delivering solid- and liquid-phase flows shows a rising trend with the increase of working flow.

Keywords: sewage pump, numerical simulation, frozen rotor method, flow characteristics

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I. INTRODUCTION

Sewage pumps consist of both solid- and liquid-phase flow pumps and are key equipment for urban channel cleanout [1~11]. Many scholars at home and abroad have carried out in-depth and meticulous research on sewage pumps and have achieved productive results. However, with the wide application of the solid-liquid pump, the shortcomings and deficiencies in the actual use were gradually exposed, such as low efficiency and excessively worn wet parts. Meanwhile, due to the complexity of two-phase flow, the theoretical research and design in this field is not mature. As the design of most existing products was based on the experiment, the designed pump performance could not be guaranteed. Therefore, studying the internal flow of the pump to provide a theoretical basis for realizing a high-performing and stable-operating pump design is needed. The present study aims to conduct a numerical simulation and analysis on solid-liquid two-phase flow pump to analyze the impact of the density of solid-phase particles on sewage pump performance, including the hydraulic performance of sewage pump and wear degree of wet parts. Through the analysis of the internal pressure and dynamic deposition distribution of particles on the surface of the solid, the basic properties of sewage pump and theoretical foundation for further design improvement could be predicted.

2 Physical model and solving method

II. PHYSICAL MODEL

The model was a medium specific speed centrifugal pump. Its basic performance parameters were as follows: flow rate $Q=50\text{m}^3/\text{h}$, head $H=20.54\text{m}$, velocity $n=2900\text{r}/\text{min}$, shaft power $P_a=3.54\text{kW}$, efficiency $\eta=79.5\%$, and net positive suction head $NPSH_C=2.59\text{m}$. The main dimensions of the pump were as follows: inlet diameter $D_j=76\text{mm}$, hub diameter $d_h=0\text{mm}$, impeller outlet diameter $D_2=137\text{mm}$, impeller outlet width $b_2=14\text{mm}$, blade outlet angle $\beta_2=30^\circ$.

2.2 Computational domain

The appropriate extension of the straight-tube suction chamber was made to eliminate the influence of the given inlet speed. An appropriate extension of the pump outlet was also carried out to better calculate convergence. As shown in Fig. 1, Tetrahedral meshes were adopted in the impeller rotation region and volute static region, with mesh numbers 435,530 and 597,127 respectively. Hexahedral meshes were used in the suction chamber and outlet extension, with mesh numbers of 152,827 and 54,944 respectively. The total mesh number of the overall computational domain was 1,240,428.

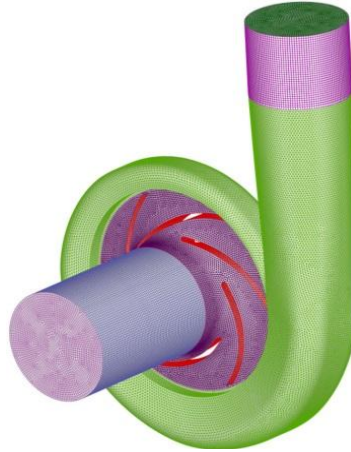


Fig.1 Computational mesh

2.3 Solved equations

According to the Boussinesq approximation,

$$-\overline{\rho u_i u_j} = \mu_t \left(\frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right) - \frac{2}{3} \left(\rho k + \mu_t \frac{\partial \bar{u}_i}{\partial x_i} \right) \delta_{ij} \quad (1)$$

Where μ_t refers to turbulent viscosity, which is the function coefficient of turbulent kinetic energy k and turbulent dissipation rate ε .

Unsteady turbulent flow calculation used in the present study used the RNG $k-\varepsilon$ two-equation model to close the mean Reynolds stress. RNG $k-\varepsilon$ turbulent model, which considers the rotation and swirling flow in the mean flow, can better process the flow with high strain rate and great streamline curvature. The RNG $k-\varepsilon$ turbulent equations are as follows:

$$\rho \frac{dk}{dt} = \frac{\partial}{\partial x_j} \left(\alpha_k \mu_{\text{eff}} \frac{\partial k}{\partial x_j} \right) + 2 \mu_t S_{ij} \frac{\partial \bar{u}_i}{\partial x_j} - \rho \varepsilon \quad (2)$$

$$\rho \frac{d\varepsilon}{dt} = \frac{\partial}{\partial x_j} \left(\alpha_\varepsilon \mu_{\text{eff}} \frac{\partial \varepsilon}{\partial x_j} \right) + 2 C_{1\varepsilon} \frac{\varepsilon}{k} \nu_t S_{ij} \frac{\partial \bar{u}_i}{\partial x_j} - C_{2\varepsilon} \rho \frac{\varepsilon^2}{k} - R \quad (3)$$

where $S_{ij} = \frac{1}{2} \left(\frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right)$; $\mu_{\text{eff}} = \mu + \mu_t$; $\mu_t = C_\mu \frac{k^2}{\varepsilon} S_{ij}$ refers to the strain rate tensor, and R refers to

ε additional source terms in the equation, representing the effect of mean strain rate ε . It is expressed as follows:

$$R = \frac{C_\mu \eta^3 (1 - \eta / \eta_0)}{1 + \beta \eta^3} \frac{\varepsilon^2}{k}, \eta = S k / \varepsilon \quad (4)$$

The model parameters in the above equations are $C_\mu=0.0845$, $C_{1\varepsilon}=1.42$, $C_{2\varepsilon}=1.68$, $\alpha_k=1.0$, $\alpha_\varepsilon=0.769$, $\beta=0.012$, and $\eta_0=4.38$.

2.4 Multiphase flow model

The general form of the ASMM is as follows, i.e., continuity equation,

$$\frac{\partial}{\partial t} (\rho_m) + \frac{\partial}{\partial x_i} (\rho_m u_{m,i}) = 0 \quad (5)$$

Where ρ_m is the density of the mixture, and u_m is the mass average velocity.

The momentum equation is

$$\begin{aligned} \frac{\partial}{\partial t} (\rho_m u_{m,j}) + \frac{\partial}{\partial x_i} (\rho_m u_{m,i} u_{m,j}) = & - \frac{\partial p}{\partial x_j} + \frac{\partial}{\partial x_i} \times \mu_m \left(\frac{\partial u_{m,i}}{\partial x_j} + \frac{\partial u_{m,j}}{\partial x_i} \right) \\ & + \rho_m g_j + \mathbf{F}_j + \frac{\partial}{\partial x_i} \left(\sum_{k=1}^n \varphi_k \rho_k u_{D,k,i} u_{D,k,j} \right) \end{aligned} \quad (6)$$

Where p is the pressure, μ_m is the effective viscosity of the mixture, g is the gravitational acceleration, F is the volume force, φ is the volume fraction, and $u_{D,k}$ is the drift velocity.

The volume fraction equation is

$$\frac{\partial}{\partial t}(\varphi_s \rho_s) + \frac{\partial}{\partial x_i}(\varphi_s \rho_s u_{m,i}) = - \frac{\partial}{\partial x_i}(\varphi_s \rho_s u_{D,s,i}) \quad (7)$$

$$\rho_m = \sum_{k=1}^n \varphi_k \rho_k \quad \mu_m = \sum_{k=1}^n \varphi_k \mu_k \quad \mathbf{u}_m = (\sum_{k=1}^n \varphi_k \rho_k \mathbf{u}_k) / \rho_m \quad (8)$$

In this study, the calculated medium is a solid-liquid two-phase flow, where $n = 2$. If a steady flow calculation is to be conducted, the phase of the local change rate will no longer exist in the above equation.

2.5 Solution settings

The dynamic and static coupling between rotor and stator in numerical calculation was achieved by means of the frozen rotor method. Velocity inlet and free output were respectively used as the boundary conditions of the inlet and outlet. Axial velocity of the pump inlet was calculated directly according to the given flow conditions and pump inlet diameter. Turbulent kinetic energy and turbulent dissipation rate under the corresponding flow were calculated based on axial velocity and pump inlet diameter. No-slip boundary condition was applied on all solid walls considering viscosity, and standard wall function was used in near-wall low Reynolds number region to deal with the problem from the high Reynolds number turbulence model. The coupling between velocity and pressure was calculated by using SIMPLE algorithm. Solid particles were uniform spherical particles with unchanged physical properties.

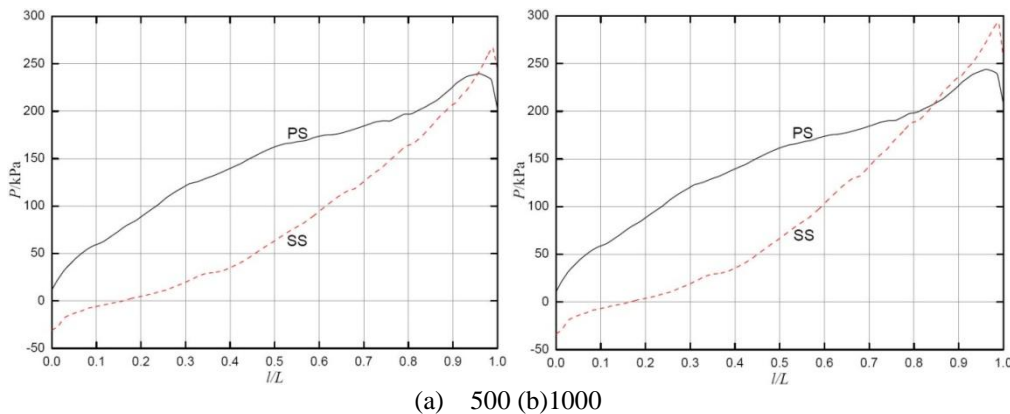
2.6 Computational scheme

Under a designed flow rate ($Q=50\text{m}^3/\text{h}$) with 10% solid-phase concentration and 0.10mm particle diameter, numerical calculation was conducted for a solid-liquid two-phase flow field under five conditions when the particle densities were 500, 1000, 1500, 2000, and 2500 kg/m^3 . Numerical calculation of the solid-liquid two-phase flow field was carried out under different working conditions: 10% solid-phase concentration, 0.10mm particle diameter, and 2500 kg/m^3 particle density.

3 Analysis of results

III. TOTAL PRESSURE DISTRIBUTION OF BLADE UNDER DIFFERENT PARTICLE DENSITIES

Fig.2 shows the total pressure distribution on the blade pressure surface and blade suction surface in five different delivering densities of solid particles. Regardless of whether on pressure surface or suction surface, total pressure increased with the increase of the blade radius. In the case of the 500 kg/m^3 density of delivering solid particles, solid-phase density was smaller than the liquid-phase density. In most areas (relative length of about 0.96), the total pressure on the blade pressure surface was higher than that on the suction surface. The total pressure on the suction surface likewise started to be higher than that on the pressure surface. In other words, position 0.96I was an isobaric equilibrium point of the pressure surface and the suction surface. For the other four densities of delivering solid particles, the changing characteristic was similarly general. The only difference was that the isobaric equilibrium points were in different positions. In the four cases of densities of delivering solid particles, i.e., 1000, 1500, 2000, and 2500 kg/m^3 , the relative positions of the isobaric equilibrium points were 0.84, 0.75, 0.72, and 0.70, respectively. Generally speaking, with the increase of delivering solid-phase density, the position of the isobaric equilibrium point was moving to the front edge of the blade.



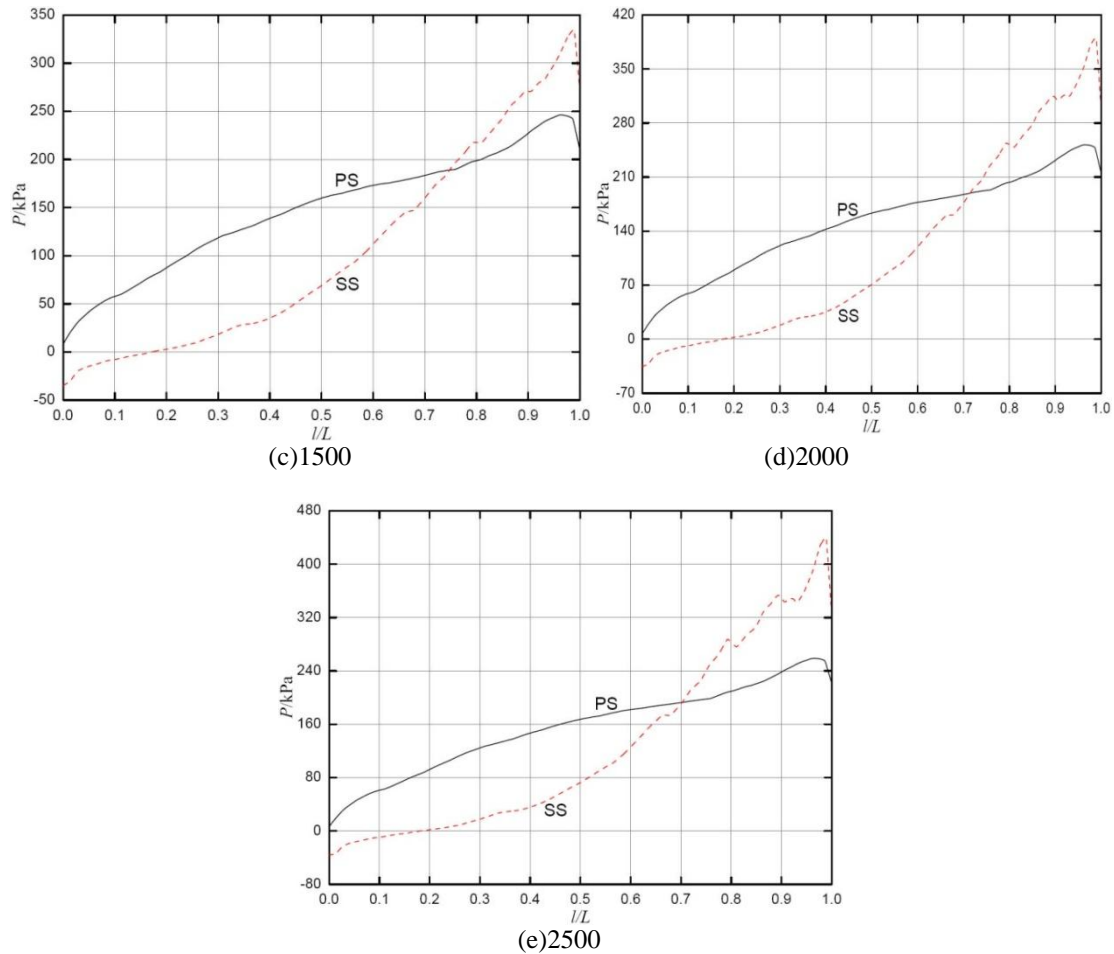


Fig.2 Distribution and variation of total pressure on the blade under different particle densities (kg/m^3)

3.2 Distribution of particle concentration of the blade under different particle densities

Fig.3 shows the distribution of solid-phase concentration on the blade pressure and suction surface under five densities of delivering solid particles. When the densities of delivering solid-phase particles were different, the difference in the concentration distribution was highly significant. When the particle density (500 kg/m^3) was smaller than the liquid-phase density (water) (1000 kg/m^3), the solid-phase concentration on the blade pressure surface was higher than that on the blade suction surface in most areas of the blade surface. This finding indicated that the blade pressure surface bore more serious wear. However, in the inlet of the blade, solid-phase concentration on the blade pressure surface was lower than that on the suction surface. Therefore, the suction surface bore more serious wear. Similarly, the position of the isoconcentration point (the point in the same radius on the blade pressure surface and the suction surface with same solid-phase concentration) was at approximately 0.11 (relative length). When particle density (1000 kg/m^3) was equal to liquid-phase density (1000 kg/m^3), the solid-phase concentration on the blade pressure surface was equal to that on the suction surface (10%) within the full range of the blade surface. This finding indicated that the blade pressure surface and suction surface bore equal wear. When particle density ($1500, 2000, \text{ and } 2500 \text{ kg/m}^3$) were greater than liquid-phase density (1000 kg/m^3), solid-phase concentration on the blade suction surface was significantly higher than that on the pressure surface in most areas on the blade surface. This result indicated that the blade suction surface bore more serious wear. However, under the latter three conditions, the position of solid-phase isoconcentration points was in 0.11, 0.13, and 0.13 (relative length). Specifically, the position of solid-phase isoconcentration point on the blade pressure and suction surface was almost unchanged with the increase of the density of delivering solid particles. This finding indicated that the degree of wear of the blade pressure surface and the suction surface did not change due to the change in particle density.

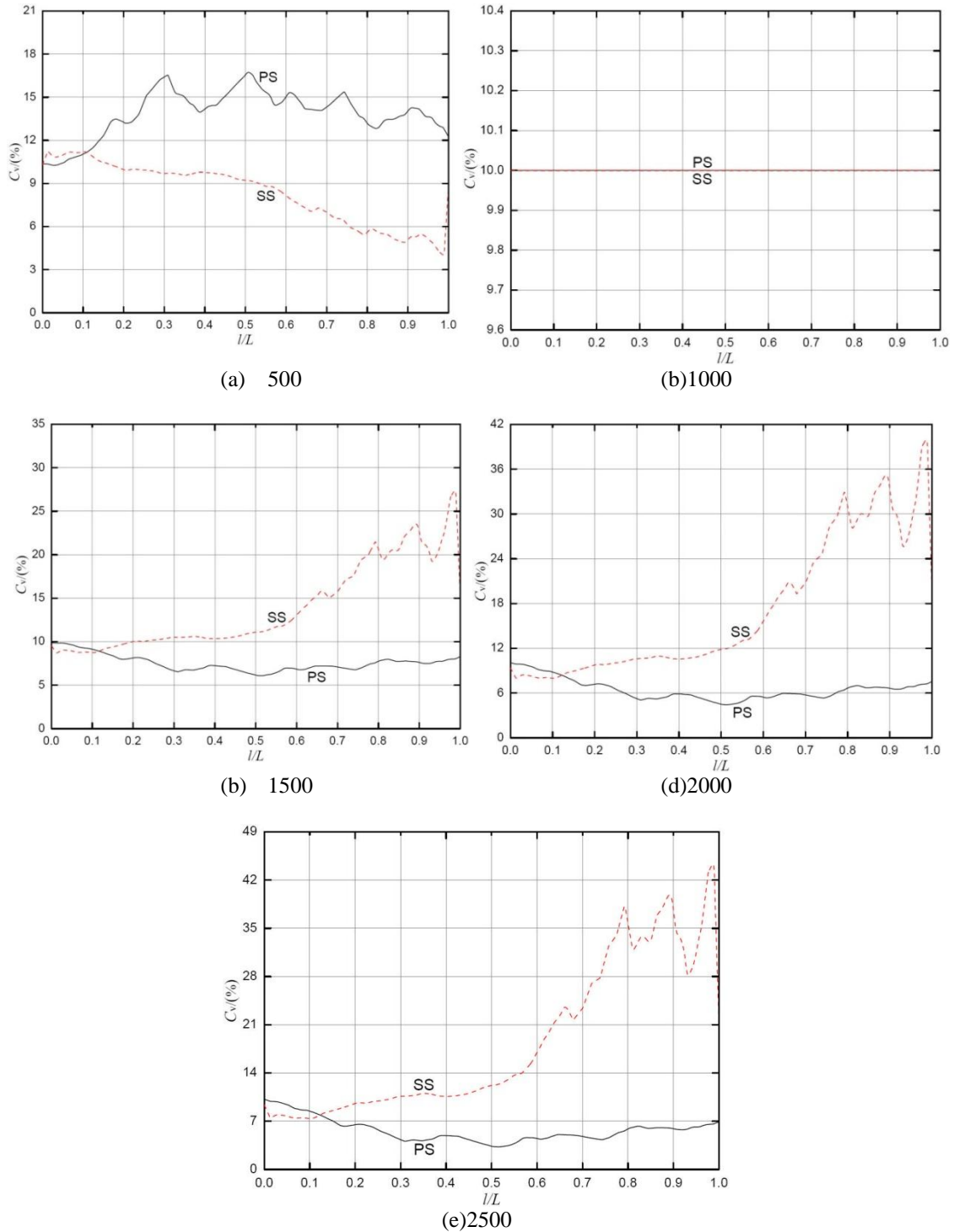


Fig.3 Distribution of particle concentrations on the blade under different particle densities (kg/m^3)

3.3 Total pressure and streamline

Fig.4 shows total pressure and streamline obtained from the calculation under different densities of delivering solid-phase particles. Under different densities of delivering solid-phase particles, streamlines in all flow channels in the impeller were not greatly different and were generally very similar. The reason was that the density of delivering solid-phase particles was different, but the calculated working condition was the designed working condition, and the corresponding internal flow conditions at that time were generally good without a significant area of stalled phenomenon.

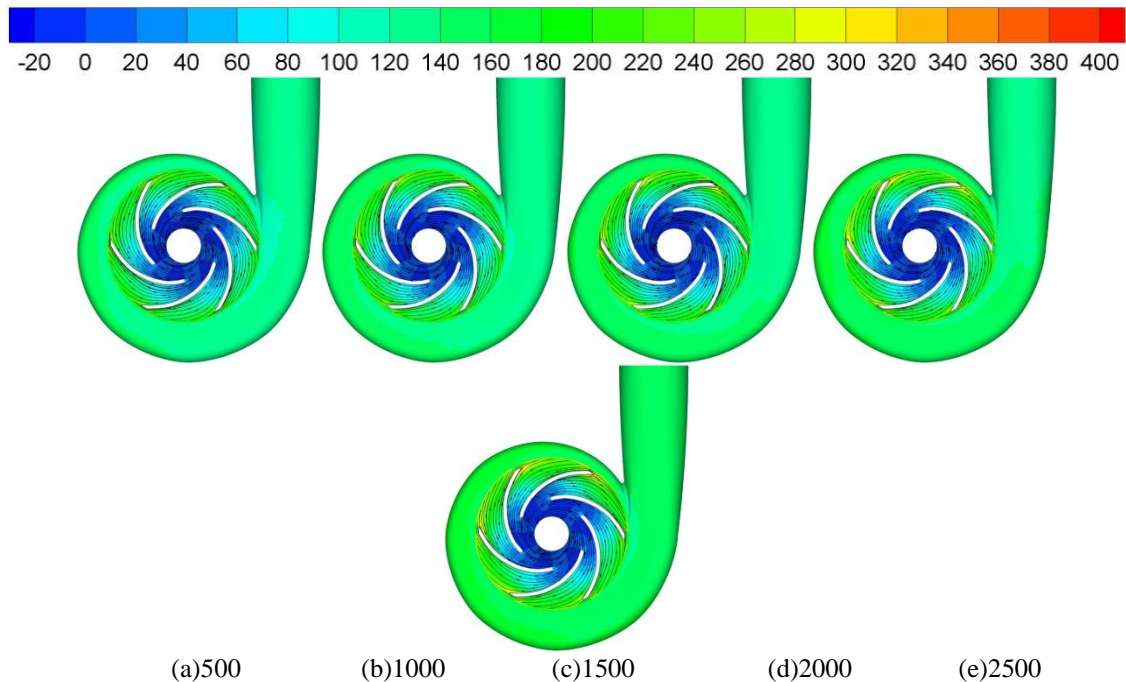


Fig.4 Distribution of total pressure and streamline under different particle densities (kg/m^3)

3.4 Difference in the external characteristics of solid-liquid two-phase flow

Under the designed working condition ($Q=50\text{m}^3/\text{h}$) and in the cases where the diameter of solid particle is 0.10mm , solid-phase delivering concentration is 10% , and the density of solid particles is 2500kg/m^3 , the flow calculation of water and solid-liquid two-phase flow was carried out. The calculation result of the external characteristics of both is shown in Fig.5. The calculation is carried out within the working condition of $0.60\text{--}1.40$ times that of rated flow. Under three working conditions that deliver flow at $30, 50,$ and $70\text{m}^3/\text{h}$, respectively, the calculation heads as delivering water medium are $22.03, 20.68,$ and 16.90m . When the calculation heads as delivering solid-liquid two-phase flow are $16.15, 13.81,$ and 7.61m , respectively, the differences under the corresponding flow between both of them are $5.88, 6.87,$ and 9.29m , respectively. Whether delivering a single-phase flow or a solid-liquid two-phase flow, hydraulic head was down with the increase of delivering flow. The hydraulic head delivering solid-liquid two-phase flow was obviously lower than that delivering water medium, and the difference between both increased with the increase of the flow rate.

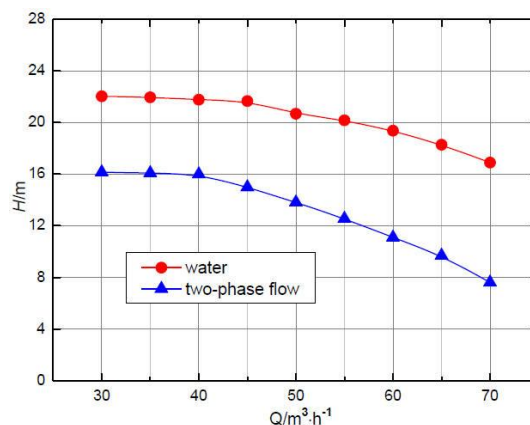


Fig.5 Comparison of external characteristics between delivering water and solid-liquid two-phase flow

3.5 Solid-phase concentration distribution

Under the same condition, solid-phase concentration distribution on the pump surface as the model pump was delivering solid-liquid two-phase flow under three working conditions (flow rates were $35, 50,$ and $65\text{m}^3/\text{h}$) is shown in Fig.6. The solid-liquid concentration distributions under three conditions were similar. This finding indicated that the degree of wear on the internal surface of the volute, the front cover, and the back cover were similar.

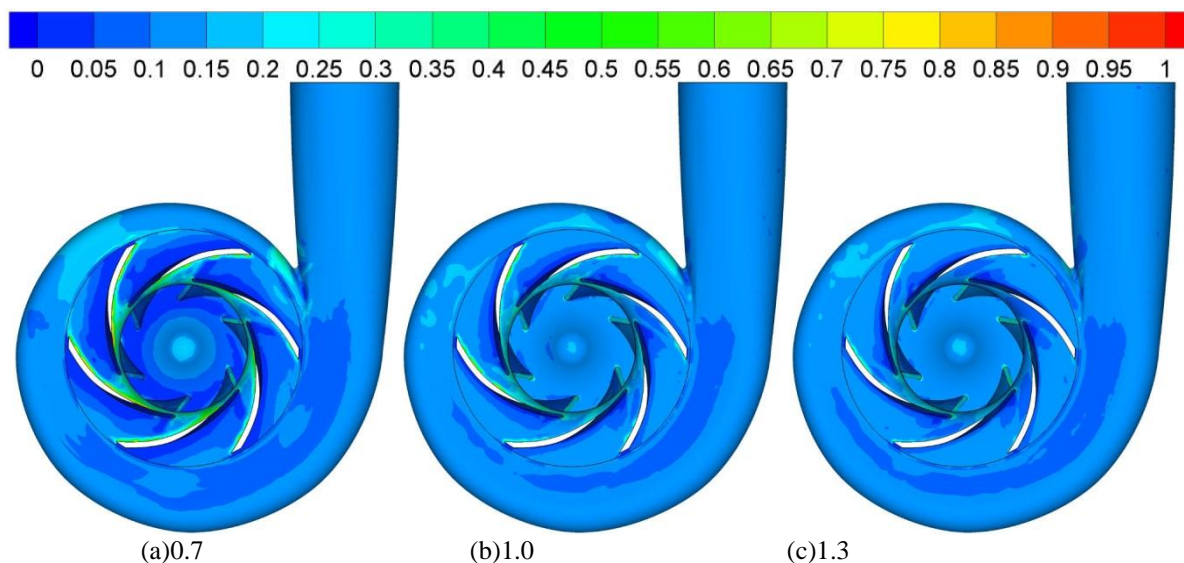


Fig.6 Solid-phase concentration distributions on pump surface(Q/Q_d)

4 Conclusions

- (1) With the increase of delivering solid-phase density, the position of isobaric equilibrium point was moving to the front edge of the blade, but the position of solid-phase isoconcentration point on the blade pressure surface and suction surface was basically unchanged. This result indicated that the wear and tear on the blade pressure surface and suction surface was not changed with the change of particle density.
- (2) Hydraulic head as delivering solid-liquid two-phase flow was significantly lower than water head, and the difference between them increased with the increase of flow rate.

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