

Revision of the Rainfall Intensity Duration Frequency Curves for the City of Kumasi-Ghana

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ABSTRACT

This work involves the revision of the Rainfall Intensity Duration Frequency (IDF) Curves for the city of Kumasi. Annual Maximum Rainfall depths of various durations over twenty-two years were obtained from the Ghana Meteorological Services. The data set was then subjected to frequency analysis to determine the distribution of which best characterize the data set. The annual maximum series were found to be drawn from the Gumbel distribution whose parameters were computed by fitting the statistics to the data. The Chi-square test and the Kolmogorov-Smirnov test prove the appropriateness of the fitting. Since the data available was only 22 years, IDF values for return periods higher than 22 years were obtained using frequency factors. The IDF estimates resulting from this work have been compared with the existing IDF curves prepared by J.B Danquah. The results show that for shorter durations (12 min and 24 min), the new IDF Curves give higher intensities for the same return period; the percentage increase ranges between 2% and 25%, while for longer durations (42min, 1 hr, 2hr, 3hr, 6hr, 12hr and 24 hr), the new IDF Curves give lower intensities for the same return period with the percentage decrease ranging between 3% and 49% when compared with the existing J.B Danquah IDF Curves. This might be as a result of low precipitation trends for shorter durations and high precipitation trends for longer durations in 1970s and before. These therefore call for the revision and updating of the existing IDF Curves for all the major cities and towns in Ghana to take into account the effect of climate change.

Keywords: IDF Curves, Gumbel Distribution, Annual Maximum Series, Climate Change, Rainfall Intensity

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I. INTRODUCTION

The design of any civil engineering infrastructure requires a comprehensive understanding of the intended purpose of the structure and the physical environment in which it would operate. In the management of storm water in a municipality, the dimensions of various components of the infrastructure system are based on the return period of heavy rainfall events. This information is often expressed as Intensity-Duration-Frequency (IDF) curves obtained from a statistical study of extreme events. The IDF curves are empirical relationships that relate the rainfall intensity, the duration and the return period in a given catchment area.

The establishment of such relationships was done as early as 1932 by Chow [1] and Dupont and Allen [2]. Since then, a lot of these curves have been developed in many parts of the world. Example Chen [3] developed a simple method to obtain a generalised rainfall IDF formula for any location in the United States using three isopleth maps of the U.S Weather Bureau. Yu et al. [4] also developed regional IDF relations for non-recording sites based on scaling theory using the hypothesis of piecewise simple scaling combined with the Gumbel distribution. In Africa, Mohymont et al. [5] assessed IDF-curves for precipitation for three stations in Central Africa and proposed more physically based models for the IDF-curves, Oyebande [6] established IDF curves for Nigeria, similarly, Dankwa [7] developed IDF curves for various towns and cities in Ghana.

The normal balance of the earth's hydrological cycle has been altered due to the changes in temperature and precipitation patterns. Projections from climate models suggest that the probability of occurrence of intense rainfall in future will increase due to the increase in green house gas emissions [8]. The design standards at present are based on historical climate information. Under a changing climate, it has become a priority for municipalities to search for appropriate procedures in the planning and management of water resources infrastructure to deal with changing climatic conditions [9].

Rainfall intensity is an important parameter for the determination of peak flow at a point in a catchment, which is used for the design of drainage structures. The IDF curves developed by Dankwa [7] is what is used in Ghana for the design of drainage structures in various cities. These IDF curves were developed based on the rainfall data

available at that time. One of the main assumptions in the creation of these curves was that the rainfall data was stationary. That is, climatic trends and variability have negligible effects on the curves. But as has been proved in recent history, climatic variability and trends do exist and their effects on precipitation have not been negligible. Climate change has led to droughts and floods around the world, and long term trends in rainfall, both increases and decreases, have been seen in different parts of the world including Ghana. There is therefore a possibility that the rainfall intensities used by Dankwa [7] for the development of the IDF curves might have changed. The IDF curves developed by Dankwa [7] have not been revised or updated, however, drainage engineers in Ghana still rely on these curves for their designs. This might lead to over-design or under-design due to the changes in climatic conditions that might have occurred after 1974. Over-designing leads to economic losses as bigger structures are designed whereas under-designing leads to drains of inadequate capacity leading to increased incidents of flooding. In both cases economic losses are incurred.

To reduce economic losses due to over design or under design of drainage structures that might occur using IDF curves developed by Dankwa [7], there is therefore the need for its revision. The main objective of this project therefore is to develop IDF curves for Kumasi based on additional available rainfall information and verify the validity of the existing IDF curves developed by Dankwa [7]. It is hoped that this research work will catapult further research works into revision and updating of the existing IDF Curves for all the major cities and towns in Ghana to take into account the effect of climate change.

II. MATERIALS AND METHODS

2.1 Study Area

Kumasi (Fig. 1) is a city in southern central Ghana's Ashanti region. Kumasi is the second largest city in Ghana also the capital of the Ashanti region.

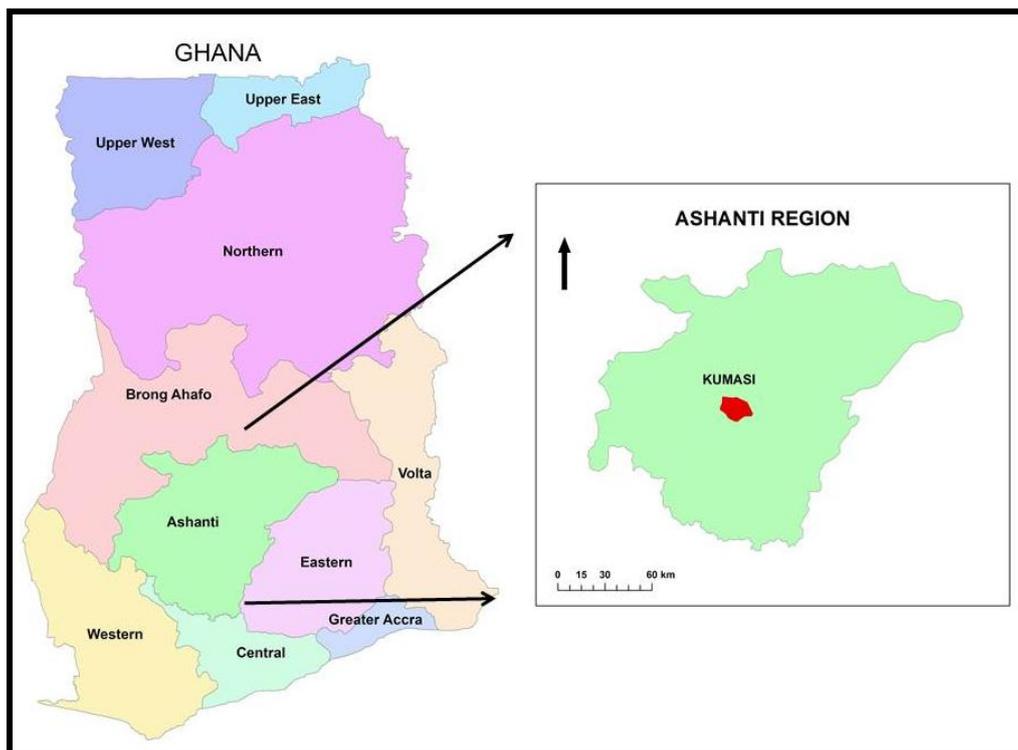


Figure1. Map of Kumasi

The climate is typically tropical, with total annual rainfall of about 1400 mm, the average maximum and minimum temperatures are about 35C and 23C which occurs in February and August respectively [10]. The potential evapotranspiration (PET) is estimated at 1450mm/y. The average humidity during the wet season is typically high (86%) and falls to about 57% in the dry period [11]. The major rivers and streams in Kumasi include Subin, Wewe, Susan, Aboabo, Oda, Owabi, Suntreso, Akribu, Acheamponmene and Asuoeyboa.

2.2 Data Collection

The data used in this study was obtained from the Ghana meteorological Services Department. The data consists of annual maximum series (AMS) of rainfall depth over a period of twenty-two years for nine (9) laps of time: 12min, 24min, 42min, 1hour, 2hours, 3hours, 6hours, 12 hours, and 24 hours.

Table 1: Summary of Data Gathered

Duration(hrs)	No. of years with some records
0.2	22
0.4	22
0.7	22
1.0	22
2.0	22
3.0	21
6.0	20
12.0	19
24.0	18

2.3 Development of IDF Curves

The data set was subjected to frequency analysis to determine the distribution of which best characterize the data set. The frequency of the rainfall is usually defined with reference to the annual maximum series, which consists of the largest values observed in each year. The annual maximum series were found to be drawn from the Gumbel distribution whose parameters were computed by fitting the statistics to the data. The fitting involves calculating the 1, 2, 5, 10, 20, 30 and 50 return intervals for each duration. Frequency precipitation P_T (in mm) for each duration with a specified return period Tr (in year) is given by:

$$P_T = P_{ave} + K S \dots\dots\dots(1)$$

Where K is the Gumbel frequency given by:

$$-\frac{\sqrt{6}}{\pi} \left\{ 0.577216 + \ln \left[\ln \frac{T}{T-1} \right] \right\} \dots\dots\dots(2)$$

For $Tr < 2$ years, K is given by:

$$-\frac{6}{\sqrt{\pi}} \times \left[0.5772 - \ln T + \frac{1}{2 \times T} + \frac{1}{24 \times T^2} + \frac{1}{8 \times T^3} \right] \dots\dots\dots(3)$$

In utilizing Gumbel's distribution, the arithmetic average in Eq. (1) is used:

$$P_{ave} = \frac{1}{n} \sum_{i=1}^n P_i \dots\dots\dots(4)$$

Where P_i is the individual extreme value of rainfall and n is the number of events or years of rainfall records.

The standard deviation (S) in equation (1) is given by:

$$S = \left[\frac{1}{n-1} \sum_{i=1}^n (P_i - P_{ave})^2 \right]^{1/2} \dots\dots\dots(5)$$

The rainfall intensity, I_T (in mm/hr) for a particular return period, T is then obtained by:

$$I_T = \frac{P_T}{t_d} \dots\dots\dots(6)$$

The IDF Curves were then developed by plotting the rainfall intensity values, I_T against corresponding durations, t_d for the different return periods.

III. RESULTS AND DISCUSSION

3.1 IDF Curves for the City of Kumasi

From the raw data, the maximum precipitation P_i and the statistical variables (average and standard deviation) for each duration, t_d (12 min, 24 min, 42 min, 60, 1 hr, 2 hr, 3 hr, 6 hr, 12 hr and 24 hr) were computed. Table 2 shows the computed frequency precipitation (P_T) values and intensities (I_T) for different return periods

Table 2: Computed frequency precipitation and Intensity values for different durations and return periods for the City of Kumasi.

Computed Precipitation (P _T) and Intensity (I _T) using Gumbel Method									
Tr (year)	Duration								
	12 min			24 min			42 min		
	Pave=26.719		S=7.786	Pave=39.629		S=12.025	Pave=44.709		S=11.248
	K	P _T	I _T (mm/hr)	K	P _T	I _T (mm/hr)	K	P _T	I _T (mm/hr)
1	-0.970	19.8	99.15	-0.970	28.0	69.9	-0.970	33.8	48.3
2	-0.164	25.4	127.2	-0.164	37.7	94.2	-0.164	42.9	61.2
5	0.719	32.3	161.6	0.719	48.3	120.7	0.719	52.8	75.4
10	1.305	36.9	184.4	1.305	55.3	138.3	1.305	59.4	84.8
20	1.866	41.3	206.3	1.866	62.1	155.2	1.866	65.7	93.9
30	2.189	43.8	218.8	2.189	66.0	164.9	2.189	69.3	99
50	2.592	46.9	234.5	2.592	70.8	177	2.592	73.9	105.5
	1 hr			2 hr			3 hr		
	Pave=59.513		S=16.547	Pave=67.162		S=20.588	Pave=66.360		S=18.568
1	-0.970	43.5	43.5	-0.970	47.2	23.6	-0.970	48.4	16.2
2	-0.164	56.7	56.7	-0.164	63.8	31.9	-0.164	63.3	21.1
5	0.719	71.3	71.3	0.719	82	41	0.719	79.8	26.6
10	1.305	81	81	1.305	94	47	1.305	90.4	30.2
20	1.866	90.3	90.3	1.866	105.6	52.8	1.866	101.1	33.7
30	2.189	95.6	95.6	2.189	112.2	56.1	2.189	107.1	35.7
50	2.592	102.3	102.3	2.592	120.6	60.3	2.592	221.7	38.2
	6 hr			12 hr			24 hr		
	Pave=66.562		S=16.789	Pave=66.578		S=21.053	Pave=59.554		S=19.393
1	-0.970	50.4	8.4	-0.970	45.6	3.8	-0.970	40.8	1.7
2	-0.164	63.6	10.6	-0.164	63.6	5.3	-0.164	55.2	2.3
5	0.719	78.6	13.1	0.719	81.6	6.8	0.719	74.4	3.1
10	1.305	88.2	14.7	1.305	93.6	7.8	1.305	84	3.5
20	1.866	97.8	16.3	1.866	105.6	8.8	1.866	96	4
30	2.189	103.2	17.2	2.189	112.8	9.4	2.189	103.2	4.3
50	2.592	109.8	18.3	2.592	121.2	10.1	2.592	110.4	4.6

The IDF Curves for the city of Kumasi were then developed by plotting the rainfall intensity values, I_T against corresponding durations, t_d for the different return periods. The IDF Curves for the city of Kumasi is presented in figure 2.

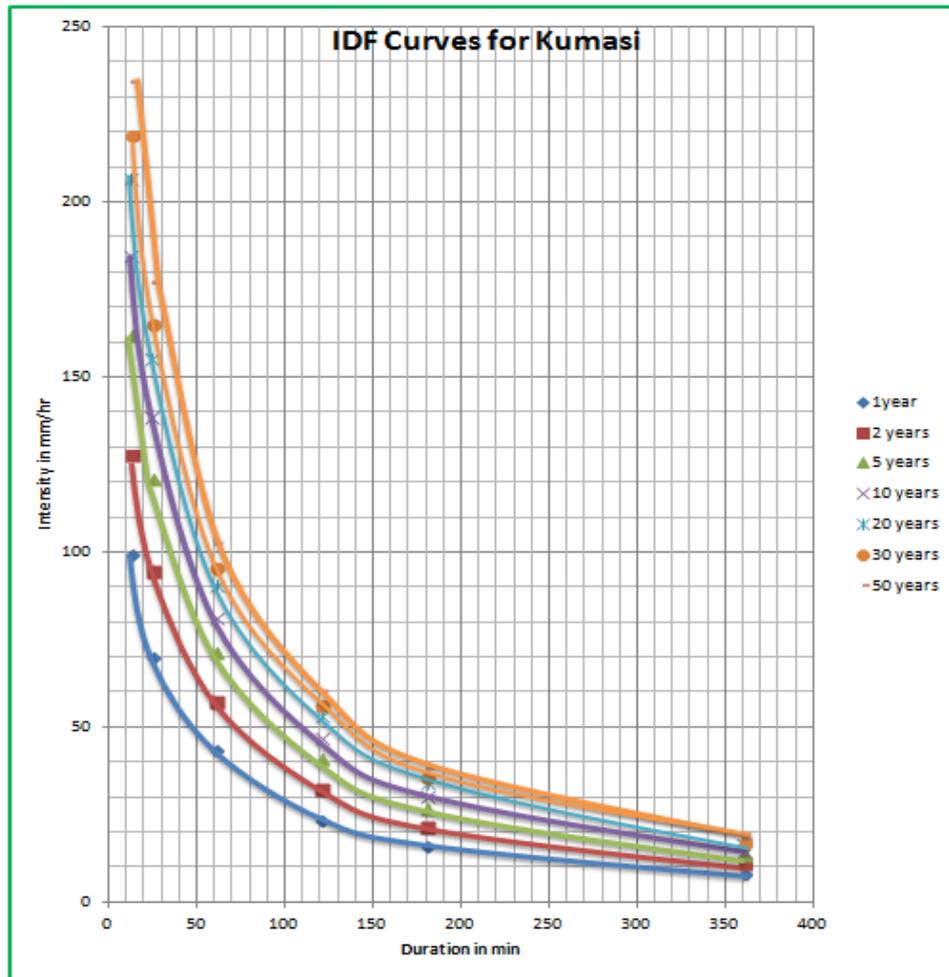


Figure2: IDF curves for Kumasi

The IDF estimates resulting from this study (Figure 2 and Table 3) are in accordance with the general properties of IDF curves. Thus for the same return period, high intensities are related to short durations and secondly, the curves are parallel; they do not cross each other.

3.2 Comparison of New IDF estimates and Existing Dankwa [7] IDF estimates for Kumasi City

Comparing the IDF results in this study to the existing Dankwa [7] IDF estimates for Kumasi, there are variations in the intensities. In order to picture the degree of variation, the new IDF estimates and the existing Dankwa [7] IDF estimates and their incremental rate of change are presented in table 3 below.

Table 3: Comparison of New IDF estimates and Dankwa [7] IDF estimates for Kumasi City

	5 Year			10 Year			25 Year			50 Year		
	ankwa	New	% incr.	Dankwa	New	% incr.	Dankwa	New	% incr.	Dankwa	New	% incr.
12 min	137.2	161.6	+17.8	153.7	184.4	+20.0	176.5	213.2	+20.8	191.8	234.5	+22.3
24 min	118.1	120.7	+2.2	127.0	138.3	+8.9	154.9	160.5	+3.6	170.2	177.0	+4.0
42 min	93.7	75.4	-19.6	104.1	84.8	-18.5	122.9	96.7	-21.3	134.9	105.5	-21.8
1hr	77.2	71.3	-7.7	83.8	81.0	-3.3	101.9	93.3	-8.4	112.0	102.3	-8.7
2hrs	45.7	41.0	-10.3	53.3	47.0	-11.8	64.8	54.6	-15.7	73.7	60.3	-18.2
3hrs	33.0	26.6	-19.4	38.6	30.2	-21.8	45.2	34.8	-23.0	50.3	38.2	-24.1
6hrs	19.3	13.1	-32.1	22.9	14.7	-35.8	27.4	16.8	-38.7	30.7	18.3	-40.4
12hrs	10.4	6.8	-34.7	12.4	7.8	-37.1	15.2	9.1	-40.1	17.3	10.1	-41.6
24hrs	5.3	3.1	-41.8	6.4	3.5	-45.3	7.9	4.1	-48.1	8.9	4.6	-48.3

The results obtained indicate that:

- The New IDF estimates are higher for shorter durations. The percentage increase ranges between 2% and 25%. This might be as a result of low precipitation trends for shorter durations in 1970s.
- New IDF estimates are lower for longer durations. The percentage decrease ranges between 3% and 49%. This might be as a result of high precipitation trends for longer durations in 1970s.

IV. CONCLUSION AND RECOMMENDATION

This work involves the revision of the Rainfall Intensity Duration Frequency (IDF) Curves for the city of Kumasi. Annual Maximum Rainfall depths of various durations over twenty-two years for Kumasi were subjected to frequency analysis to determine the distribution of which best characterize the data set. The annual maximum series were found to be drawn from the Gumbel distribution whose parameters were computed by fitting the statistics to the data. The Chi-square test and the Kolmogorov-Smirnov test prove the appropriateness of the fitting.

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These therefore call for the revision and updating of the existing Dankwa [7] IDF Curves for all the major cities and towns in Ghana to take into account the effect of climate change.

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