

## Classical mechanics analysis of the atomic wave and particulate forms

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### ABSTRACT

Physical properties of the atom's intrinsic electromagnetic (e-m) harmonic oscillation are analyzed with SHM formalism. The results would suggest that light does not travel in the sense of rectilinear motion, it is an oscillating e-m loop of cosmic proportions and rotates as it radiates. It is re-affirmed that the atom exists simultaneously as wave and as particle, each characterized by specific physical properties and further revealed that: (i) waveforms of the chemical elements bind together into a perfect superfluid to constitute space (i.e., the "vacuum") as such physical properties of the vacuum are summations of properties of each element's waveform and comprise values of atomic radius, density, angular speed, centripetal force and modulus analogous to corresponding values of the visible elements; (ii) waveform densities add up to  $2.608889474 \times 10^{-36} \text{ kg/m}^3$ ; the value confirms existence of the long speculated vacuum energy; given the density, cosmological constant evaluates at  $\Lambda = 7.2955513855 \times 10^{-52} \text{ m}^{-2}$  confirming the observed value  $\sim 10^{-52} \text{ m}^{-2}$ ; (iii) the combined  $\lambda$  values of the wave and particulate forms gives rise to the e-m spectrum; (iv) radioactivity results from changes in tensile properties of the atom as atomic number increases, it is an exclusive phenomenon of the microcosmic atom, the visible macrocosmic particulate form plays no role whatsoever; (v) the results would suggest that atomic wave and particulate forms are identifiable with bosons and fermions respectively.

Keywords: Atomic Classical (Newtonian) Mechanics; Physical Properties; Simple harmonic motion; Radioactivity.

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### I. INTRODUCTION

As presently constituted quantum physics rests on a speculative foundation hence we have now reached the point where advances in empiricism throw up realities that question the basis of that foundation. Our investigation of the subject suggests the necessity for a major paradigm shift that would address the unknown from the well known and we submit that despite phenomenal advances in technology and the underlying theoretical framework, with regard to the atom, physics has only one positively known - relative atomic mass  $m_r$ . Knowledge of the phenomenon that specifies values of this known should lead to a better understanding of other properties of the atom. Since Lorentz's seminal treatises [1], there have been several theoretical constructs for atomic mass; notably, de Broglie's re-interpretation [2] of the combined energy equations of Planck [3] and Einstein [4]. In our context the equation,

$$h\vartheta = mc^2, \quad (1)$$

assigns to each element specific e-m field  $\vartheta$  and inertial mass  $m$  values. We were unable to find a reported attempt to evaluate  $m$  with eq. (1) and recognize that physics is yet to provide relevant values of  $\vartheta$ . Although tentative values were published in 1957 [5], they have been ignored on seemingly justifiable grounds. We decided nonetheless to attempt evaluating  $m_r$  by first substituting the published  $\vartheta$  values in (1) to obtain each element's absolute atomic mass  $m_{\text{abs}}$  (or  $m_w$ ) value. The result was completely unexpected, in contrast with an approx. linear trend observed for empirical  $m_r$ , values of  $m_w$  increase exponentially with an increase in atomic number  $Z$ . In order to reproduce  $m_r$  from  $m_w$  values, it became necessary to conceive of three frames of reference for the atom. The simplest empirical model (tagged "Lever System Cosmological Model") that successfully describes this structure yields striking results that perfectly corroborate values of some established physical constants but differ markedly in perception of the causalities. It turned out, for instance, that the atom exists simultaneously in the micro- and macrocosms in three mutually orthogonal domains. In the macrocosm it exists only as wave-embedded particles; however, the microcosm comprises both wave and wave-embedded particles. The wave is characterized by absolute not relative atomic mass values, it is the only form for which

eq. (1) is strictly applicable. These results have been reported [6,7]; here, we present results of analysis of the atom's wave – particle dual existence within the context of its physical properties.

## II. EVALUATION OF PHYSICAL PROPERTIES OF THE ATOM

If, as has been proposed [5,8,9] and demonstrated [6,7] the atom is essentially an e-m field, it should be describable with established formalisms of simple harmonic motion (SHM) and the following quantitative expressions would apply:

i. Radius,  $r = \lambda/2 = c/2\vartheta$  (2)

where the wavelength  $\lambda = c/\vartheta$ , and values of  $\vartheta$  and  $c$  depend on the atom's specific wave or particulate form.

ii. Density,  $\rho = m/v = m/(4\pi r^3/3) = 6m\vartheta^3/\pi c^3$ , (3)

where values of mass  $m$  and volume  $v$  depend also on the atom's specific form.

iii. Angular speed,  $\omega = 2\pi\vartheta$ , (4)

iv. Centripetal Force,  $F = m\omega^2 r = 8\pi^2 m\vartheta^3/c$ , (5)

v. Elastic Modulus,  $\epsilon = m\omega^2 = 4\pi^2 m\vartheta^2$ , (6)

vi. Longitudinal Stress,  $\sigma = F/\pi r^2 = 8\pi m\vartheta^3/c$  (7)

vii. Strain rate,  $\tau = \sigma/\epsilon = 2\vartheta/\pi c = \omega/\pi^2 c$  (8)

Results of these calculations are presented.

## III. RESULTS AND DISCUSSION

Values of the physical properties calculated with eqs. (2) to (8) are summarized in Table 1 for the chemical elements, the details are illustrated in Figs. 1 to 7. Table 1 contains three sections that present properties of the various forms of the atom: (1) Absolute Ref. Frame's microcosmic waveform  $U_{abs}^*$ ; (2) Visible Ref. Frame's macrocosmic particulate form  $U^o$ ; and (3) Invisible relative component of the Absolute ref. frame  $U_r^*$ , plus Invisible Analogue  $U'_r$  of the Visible Frame, both having microcosmic particulate matter. The ref. frames are co-existent, orthogonal, interactive and freely exchange inertial mass and energy; they are defined by the same set of chemical elements undergoing the same periodicity, as a result we have tagged them parallel universes [6,7]. The results show clearly that each form is characterized by its specific de Broglie wavelength defined by eq. (1). The waveform's absolute atomic mass  $m_w^*$  (or  $m_{abs}^*$ ) varies from  $7.37 \times 10^{-51}$  to  $4.75 \times 10^{-41}$  kg/atom for electron  $e$  to americium  $Am$  respectively. The value  $7.37 \times 10^{-51}$  kg/atom compares reasonably with  $10^{-53}$  kg/atom postulated by de Broglie [2] and  $\sim 10^{-54}$  kg/atom speculated recently as experimental limit for the photon [10]. For the visible universe  $U^o$ , molar mass  $m^o$ , values vary across the periodicity from  $9.77 \times 10^{-7}$  to  $0.234$  kg/mol for  $Ab$  to  $Am$  respectively [6,7]. With this brief background we discuss the present results.

### A. Radius of the non-bonded neutral isolated atom

Atomic waveform's radius  $r_w$  varies from  $1.4990 \times 10^8$  to  $2.3267 \times 10^{-2}$  m for Russell's first element "alberton"  $Ab$  to americium  $Am$  respectively, Table 1. Corresponding values for the visible particulate molar unit  $r_p^o$  are  $9.1312 \times 10^{-15}$  to  $3.6696 \times 10^{-20}$  m respectively. Likewise, corresponding values for the microcosmic particulate form  $r_p^*$  (or  $r_p'$ ) are  $1.8262 \times 10^{-14}$  to  $2.8349 \times 10^{-24}$  m for  $Ab$  to  $Am$  respectively. Note that these values refer to the non-bonded neutral isolated individual atom completely free of influence of a field other than its own. This form of the atom was hitherto inaccessible to physics and this is possibly the first time its physical properties are being reported. The value  $r_{w(Ab)} = 1.4990 \times 10^8$  m is of course  $\lambda/2$ , where  $\lambda = c/\vartheta$ ,  $\vartheta = 1.0$  Hz [6,7] and  $c$  is the transverse vacuum radiation;  $r_w$  therefore positively identifies  $Ab$ 's waveform with the long wave end of the e-m spectrum. Observe also that the visible atom's particulate  $Ab$ 's radius  $r_{p(Ab)} = 9.1312 \times 10^{-15}$  m compares well with the "classical electron radius" (CER)  $r_e = 2.8179 \times 10^{-15}$  m despite a wide margin between the electron mass  $m_e$  value obtained here  $7.37 \times 10^{-51}$  kg and literature value  $9.11 \times 10^{-30}$  kg. Thus,  $r_{p(Ab)}$  is positively identified here with the electron  $e$  re-affirming that Russell's  $Ab$  is indeed the electron. In previous reports we also identified  $Ab$  with  $e$  on the basis of similarity of relative atomic mass values [6] and correspondence between values of  $h$  and  $e$ 's internal energy [7].  $Ab$  is first element of Russell's periodicity, its positive identification with  $e$  would support our earlier submission [6] that  $e$  is a full-fledged element on its own merit and is indeed the first member of the chemical periodicity; there is a large volume of literature to buttress this position [11-14]. For the neutral isolated atom,  $r$  value decreases with an increase in atomic number  $Z$  notably, the same trend is observed for the wave and particulate forms regardless of cosmic domain Fig. 1. The literature presents the contrary, i.e., empirical  $r$  values increase generally with an increase in  $Z$  value [15-17]. We submit that effects responsible for observed increase in  $r$  value along the periodicity such as shielding (18) arise from the chemical (i.e., e-m [1]) environment and are not intrinsic nature of the isolated atom. For instance, we find four orders of magnitude difference between literature's covalent H-H radius of molar hydrogen  $r_{H-H} = 2.5 \times 10^{-11}$  m [15,16] as against the present value  $r_H = 9.1 \times 10^{-15}$  m for the isolated non-bonded H-atom.

It is not unlikely that if r values were not thus enlarged significantly, tangible matter and gravity would have been absolutely intractable. The electron's waveform radius  $r_{e(w)} = 1.4990 \times 10^8$  m is significant, cosmological dimensions are measured in units of the light year, however, in the SHM context light does not translocate, it is an e-m wave oscillating within the cosmic envelope with  $\lambda = c/9 = 2.99792458 \times 10^8$  m ( $\mathcal{G}_{Ab} = 1.0$  Hz [5]).

TABLE 1: A summary of some physical properties of the elements

Atom	At. Radius r/m	At. Density $\rho/\text{kg m}^{-3}$	Angular Speed $\omega/\text{rad s}^{-2}$	Centripetal Force F/N	Elastic Modulus $\epsilon/\text{Pa}$	Longtd. Stress $\sigma/\text{Pa}$	Strain Value $\tau$
Absolute Ref. Frame - microcosmic waveforms							
Ab(e)	1.4990E+08	5.2258E-76	4.1917E-08	4.3628E-41	2.9105E-49	6.1806E-58	2.1235E-09
H	7.3192E+04	9.1933E-63	1.7581E-01	1.8299E-34	2.5001E-39	1.0873E-44	4.3490E-06
C	9.1489E+03	3.7656E-59	1.1252E+01	1.1711E-32	1.2801E-36	4.4536E-41	3.4792E-05
Si	1.1436E+03	1.5424E-55	7.2013E+02	7.4952E-31	6.5540E-34	1.8242E-37	2.7834E-04
Fe	7.1476E+01	1.0108E-50	1.8435E+05	1.9188E-28	2.6845E-30	1.1955E-32	4.4534E-03
Br	3.8121E+01	1.2493E-49	6.4811E+05	6.7457E-28	1.7696E-29	1.4776E-31	8.3501E-03
Ba	1.1168E+00	1.6959E-43	7.5511E+08	7.8593E-25	7.0373E-25	2.0057E-25	2.8502E-01
Ta	2.5071E-01	6.6774E-41	1.4984E+10	1.5595E-23	6.2203E-23	7.8974E-23	1.2696E+00
Rn	1.3960E-01	6.9463E-40	4.8327E+10	5.0300E-23	3.6031E-22	8.2155E-22	2.2801E+00
U	3.1023E-02	2.8484E-37	9.7862E+11	1.0186E-21	3.2833E-20	3.3689E-19	1.0261E+01
Am	2.3267E-02	9.0024E-37	1.7398E+12	1.8108E-21	7.7827E-20	1.0647E-18	1.3681E+01
Visible Ref. Frame - macrocosmic particulate forms							
Ab(e)	9.1312E-15	3.0622E+35	1.3999E+15	1.4570E-18	1.5957E-04	5.5625E+09	3.4860E+13
H	4.4586E-18	5.3871E+48	5.8716E+21	6.1113E-12	1.3707E+06	9.7857E+22	7.1393E+16
C	7.4248E-19	7.0050E+51	2.1173E+23	2.2037E-10	2.9681E+08	1.2725E+26	4.2871E+17
Si	3.1745E-19	2.0962E+53	1.1582E+24	1.2055E-09	3.7975E+09	3.8078E+27	1.0027E+18
Fe	1.5966E-19	3.2759E+54	4.5787E+24	4.7656E-09	2.9848E+10	5.9507E+28	1.9936E+18
Br	1.1160E-19	1.3722E+55	9.3711E+24	9.7537E-09	8.7395E+10	2.4926E+29	2.8521E+18
Ba	6.4932E-20	1.1976E+56	2.7684E+25	2.8814E-08	4.4376E+11	2.1754E+30	4.9022E+18
Ta	4.9280E-20	3.6097E+56	4.8063E+25	5.0025E-08	1.0151E+12	6.5570E+30	6.4593E+18
Rn	4.0167E-20	8.1780E+56	7.2344E+25	7.5297E-08	1.8746E+12	1.4855E+31	7.9246E+18
U	3.7462E-20	1.0808E+57	8.3169E+25	8.6564E-08	2.3107E+12	1.9634E+31	8.4968E+18
Am	3.6696E-20	1.1740E+57	8.6678E+25	9.0217E-08	2.4585E+12	2.1325E+31	8.6742E+18
Abs. Ref. Frame, Relative Compont.- microcosmic particulate forms							
Ab(e)	1.8262E-14	1.9139E+34	3.4998E+14	3.6426E-19	1.9946E-05	3.4766E+08	1.7430E+13
H	8.9171E-18	3.3669E+47	1.4679E+21	1.5278E-12	1.7134E+05	6.1161E+21	3.5696E+16
C	2.2237E-18	8.7058E+49	2.3604E+22	2.4568E-11	1.1048E+07	1.5814E+24	1.4314E+17
Si	2.4832E-19	5.5988E+53	1.8929E+24	1.9702E-09	7.9340E+09	1.0170E+28	1.2819E+18
Fe	9.2105E-21	2.9580E+59	1.3759E+27	1.4321E-06	1.5548E+14	5.3733E+33	3.4559E+19
Br	4.8460E-21	3.8601E+60	4.9703E+27	5.1732E-06	1.0675E+15	7.0119E+34	6.5685E+19
Ba	1.3635E-22	6.1590E+66	6.2782E+30	6.5345E-03	4.7924E+19	1.1188E+41	2.3345E+21
Ta	3.0564E-23	2.4394E+69	1.2495E+32	1.3005E-01	4.2549E+21	4.4313E+43	1.0414E+22
Rn	1.7015E-23	2.5397E+70	4.0315E+32	4.1961E-01	2.4661E+22	4.6133E+44	1.8707E+22
U	3.7800E-24	1.0428E+73	8.1691E+33	8.5026E+00	2.2494E+24	1.8942E+47	8.4210E+22
Am	2.8349E-24	3.2960E+73	1.4524E+34	1.5116E+01	5.3323E+24	5.9872E+47	1.1228E+23

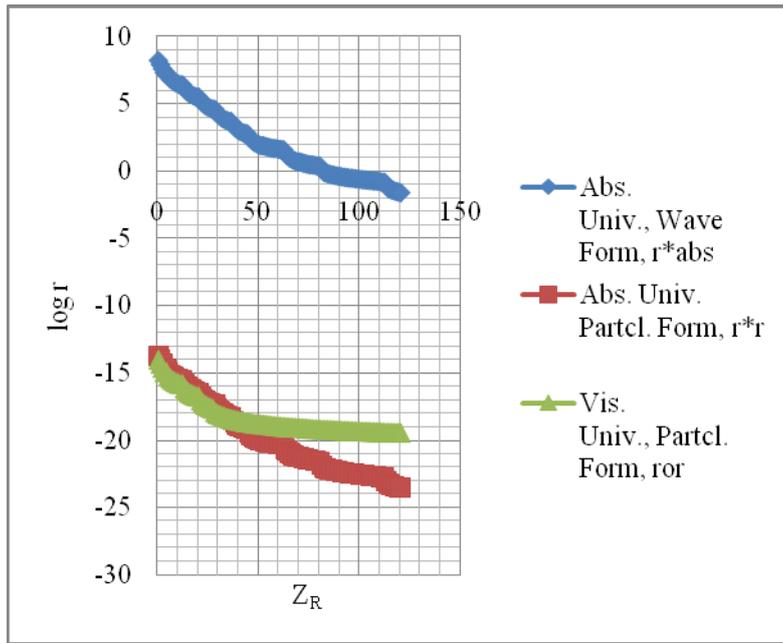


Fig. 1 Plot of atomic radius log r vs. atomic no.  $Z_R$

The value of  $r_{e(w)}$  implies therefore that distances covered by light actually represent accessible extents of  $e$ 's waveform envelopes. Thus, although it has non-zero mass, the photonic envelope can and does oscillate at angular speeds greater than light without violating quantum restrictions [19] and we find in Table 1 speeds in excess of  $10^{10}$  rads/s. Plots of  $r$  vs.  $Z$  are parabolic (Fig. 1), attempts to 'linearize' these curves revealed that variations of all atomic physical parameters with  $Z$  are strictly non-linear. For instance, a plot of  $\sqrt{\vartheta}$  vs.  $Z$  yields the expression  $\vartheta = \{6.68(Z - 6.0524)\}^2$  with  $R^2 = 0.98$ , i.e., the graph is a best fit not the perfect straight line obtained by Thomson [20] suggesting that the present investigation addresses a different level of the atom's e-m radiation. The log-log correlation illustrated in Fig. 2 proved quite invaluable, the procedure produced a resourceful range of linear correlations that would take quite a while to fully investigate.

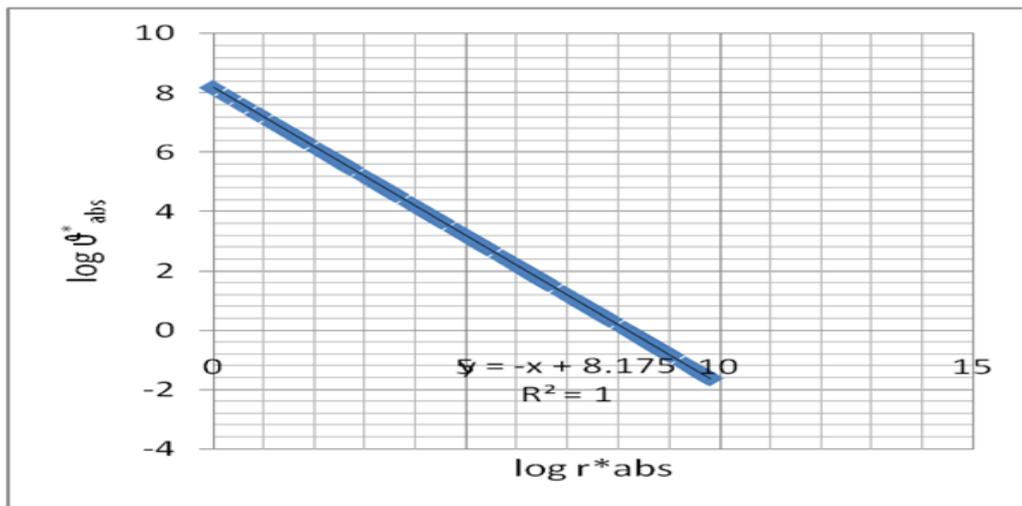


Fig. 2: Plot of  $\log \vartheta_{abs}^*$  vs.  $\log r_{abs}^*$  – waveform

For instance, Fig. 2 gives the following correlation of  $\vartheta$  with  $r$ :

$$\vartheta = A_1/r \tag{9}$$

where  $A_1 = 1.4962235656 \times 10^8$  for waveform and  $1.862087173 \times 10^{-14}$  m for particulate atom; these values are easily recognizable as graphical estimates of  $r_{e(w)}$  and  $r_{e(p)}$  respectively. Notably, the molar value  $r_{e(p)}^* = 1.86209 \times 10^{-14}$  m corroborates our earlier submission that it refers to the cosmic microwave background (CMB) [6,7]; furthermore, it is shown in Table 2 that the combined radii of the wave and particulate forms gives rise to the e-m spectrum.

TABLE 2: Comparison of atomic  $\vartheta$  and  $\lambda$  values with e-m spectrum

Russ. Period	Russell's Element	Russ. Atm. No. Z <sub>R</sub>	Atomic e-m Freq. $\vartheta_{At.}/\text{Hz}$	Atomic Wave length $\lambda_{At.}/\text{m}$	Literature e-m Spec. $\vartheta_{e-m}/\text{Hz}$	Literature e-m Spec. $\lambda_{e-m}/\text{m}$	Source /Use
<u>Microcosmic Atomic Waveform</u>							
1	Ab = e	1	1.0	2.9979E8	1	10 <sup>8</sup>	Long
2	Bl – En	2 – 6	2 -16	1.5 - 1.9E8	2 -10	10 <sup>8</sup> - 10 <sup>7</sup>	Waves
3	Ey – Vt	7 – 15	24 – 192	1.2E7 - 1.6E6	10 - 10 <sup>2</sup>	10 <sup>7</sup> - 10 <sup>6</sup>	Audio
4	Ou – H	16 – 24	256 -2048	1.2E6 - 1.6E5	10 <sup>2</sup> -10 <sup>3</sup>	10 <sup>6</sup> -10 <sup>5</sup>	Waves
5	L – O	25 -34	2.5E3 - 2.4E4	9.8 - 1.0E4	10 <sup>3</sup> -10 <sup>4</sup>	10 <sup>5</sup> - 10 <sup>4</sup>	
6	F – Ar	35 – 44	2.9E4 - 2.6E5	9.1 - 1.1E3	10 <sup>4</sup> - 10 <sup>5</sup>	10 <sup>4</sup> -10 <sup>3</sup>	Radio
7	K – Cu	45 – 55	2.6E5 - 2.6E6	572- 102	10 <sup>5</sup> -10 <sup>6</sup>	10 <sup>3</sup> - 10 <sup>2</sup>	
8	Zn – Mo	56 -68	2.9E6 - 2.5E7	95.3 - 10.2	10 <sup>6</sup> -10 <sup>7</sup>	10 <sup>2</sup> -10	Waves
9	Tc – Pr	69 -85	2.9E7 - 2.5E8	8.93 - 1.08	10 <sup>7</sup> - 10 <sup>8</sup>	10 - 10 <sup>-1</sup>	Micro-
10	Nd – Fr	86 – 113	2.8E8 - 1.1E9	0.984 - 0.140	10 <sup>8</sup> -10 <sup>9</sup>	10 <sup>-1</sup> - 10 <sup>-2</sup>	
1	Ra – Am	114 -121	2.2 - 6 44E9	0.093 - 0.047	10 <sup>9</sup> - 10 <sup>10</sup>	10 <sup>-2</sup> - 10 <sup>-3</sup>	Waves
					10 <sup>10</sup> -10 <sup>22</sup>	10 <sup>-4</sup> - 10 <sup>-13</sup>	IR, V, UV, X- & $\gamma$ - Rays
<u>Micro/Macrocosmic Atomic Particulate Form</u>							
1	e – Bl	1 – 2	1.02 - 2.03	3.7 - 1.8E-14	10 <sup>22</sup> - 10 <sup>23</sup>	10 <sup>-14</sup> - 10 <sup>-15</sup>	Gamma
2	Bs – Ah	3 – 8	4.07 -32.55	9.1E-14 - 1.1E-15	10 <sup>24</sup> - 10 <sup>25</sup>	10 <sup>-15</sup> - 10 <sup>-16</sup>	Rays
3	Bd – Tr	9 – 17	40.69 - 325.5	9.1E-15 - 1.1E-16	10 <sup>25</sup> - 10 <sup>26</sup>	10 <sup>-16</sup> - 10 <sup>-17</sup>	$\alpha$ -
4	Bz – Ng	18 -27	3.9E2 - 3.7E3	9.5-16 - 1.0E-17	10 <sup>26</sup> - 10 <sup>27</sup>	10 <sup>-17</sup> - 10 <sup>-18</sup>	
5	He – Na	28 -37	3.7E3 - 3.3E4	8.9E-17 - 1.1E-18	10 <sup>27</sup> - 10 <sup>28</sup>	10 <sup>-18</sup> - 10 <sup>-19</sup>	Particles
6	Mg – K	38 – 45	6.7E4 - 2.7E5	5.6E-18 - 1.4E-19	10 <sup>28</sup> - 10 <sup>29</sup>	10 <sup>-19</sup> - 10 <sup>-20</sup>	
7	Ca – As	46 – 59	5.3E5 - 3.5E6	7.0E-19 - 1.1E-20	10 <sup>29</sup> - 10 <sup>30</sup>	10 <sup>-20</sup> - 10 <sup>-21</sup>	High
8	Se – Rh	60 -71	3.7E6 - 8.4E7	9.9E-20 - 1.1E-21	10 <sup>30</sup> - 10 <sup>31</sup>	10 <sup>-21</sup> - 10 <sup>-22</sup>	Energy
9	Pd – Eu	72 – 89	3.8E7 - 3.6E8	9.7E-21 - 1.0E-22	10 <sup>31</sup> - 10 <sup>32</sup>	10 <sup>-22</sup> - 10 <sup>-23</sup>	$\alpha$ -
10	Gd – Ac	90 - 115	3.9E8 - 3.3E9	9.6E-22 - 1.1E-23	10 <sup>32</sup> - 10 <sup>33</sup>	10 <sup>-23</sup> - 10 <sup>-24</sup>	
1	Th – Am	116 -121	3.8E 8- 6.6E9	9.7E-23 - 5.7E-24	10 <sup>33</sup> - 10 <sup>34</sup>	10 <sup>-24</sup>	Particles

**B. Other atomic physical properties**

The waveform density  $\rho_w^*$  varies from  $5.23 \times 10^{-76}$  to  $9.00 \times 10^{-37}$  kg/m<sup>3</sup> for e to Am respectively; on the other hand, the isolated particulate atom is possibly the densest object in the cosmos. Values of  $\rho_p^0$  vary from  $3.1 \times 10^{35}$  to  $1.2 \times 10^{57}$  kg/m<sup>3</sup> for macroscopic visible e to Am respectively, while corresponding values for the microcosmic (i.e., vacuum) analogues are:  $\rho_p^* \cong \rho_p^0 = 1.8 \times 10^{34}$  to  $2.8 \times 10^{73}$  kg/m<sup>3</sup>. For reason of space we are unable to present a detailed comparison between values of radiation densities of the vacuum obtained here and those predicted in cosmological models. Briefly, we note that unlike visible particulate forms, atomic waveforms are firmly held together by gravity as a result, the vacuum exists as a single cosmic superfluid, i.e., the photon [21]. Although each element retains its specific physical properties in the fluid, measurement would yield not the individual but sum total vacuum density  $\rho_{vac} = 2.608889474 \times 10^{-36}$  kg/m<sup>3</sup> in reasonable agreement with the predicted values: Lemaitre,  $\rho_{vac} \sim 10^{-30}$  [22]; Einstein and de Sitter,  $\sim 10^{-31}$  [23]; and Alpher and Herman,  $\sim 10^{-35}$  [24]. It is important to note that the present value represents not the critical but *actual* vacuum density; notably, it confirms existence of the long speculated vacuum energy and yields  $\Lambda = 8\pi\rho_{vac}G/c^2 = 7.2955138855 \times 10^{-52}$  m<sup>-2</sup> in line with the observed value of  $\sim 10^{-52}$  m<sup>-2</sup>. The SHM parameters: angular speed  $\omega$ ; centripetal force F; elastic modulus  $\epsilon$ ; longitudinal stress  $\sigma$  and strain  $\tau$  are presented within the context of radioactivity.

### C. Classical mechanics perspective of radioactivity

A summary of values of the atom's SHM parameters is presented in cols. 4 to 8, Table 1; the complete trends are illustrated in Figs. 3 to 10. The values follow the characteristic parabolic trend with an increase in Z, the details are examined.

#### 1. Angular Speed

The waveform spins with angular speed  $\omega_w$  that varies from 6.28 to  $4.05 \times 10^{10}$  rad/s for e to Am respectively while values for the corresponding macro- ( $\omega_p^o$ ) and microscopic particulate forms  $\omega_p^*$  and  $\omega_p'$  are  $12.78$  to  $3.18 \times 10^6$  and  $6.39$  to  $4.12 \times 10^{10}$  rads/s respectively. We find here a clear indication that light spins at 6 rad/s as it radiates. From phosphorous P ( $Z_R = 41$ ) to Am ( $Z_R = 121$ ) the waveforms execute angular speeds in excess of a million rad/s with values rising incredibly to billions of rad/s along the periodicity. Observe that the wave and particulate forms spin independently and at different speeds; the difference becomes increasingly pronounced beginning with the element Ne ( $Z_R = 36$ ) which marks onset of Russell's 5<sup>th</sup> period. The results support our earlier observation that a major structural change occurs at Russell's 5<sup>th</sup> period, i.e., "octave" and that the three ref. frames ( $U_r^*$ ,  $U_r^o$  and  $U_r'$ ) are mutually independent (orthogonal) yet interactive [6,7].

#### 2. Other SHM Parameters

Values of the waveform's centripetal force  $F_w^*$  vary from  $4.36 \times 10^{-41}$  to  $1.81 \times 10^{-21}$  N for e to Am respectively; these values, of course, refer to the range of centripetal forces operating within the vacuum. For corresponding particulate forms we have  $F_p^o = 1.46 \times 10^{-18}$  to  $9.02 \times 10^{-8}$  N and  $F_p' \cong F_p^* = 3.64 \times 10^{-19}$  to 15.12 N. Despite these predominantly low values, F plays key roles that decide major properties of the atom for instance, its interactions with atomic mass, strain and density give rise to gravitation, electricity and magnetism respectively. Strain rate  $\tau$  on the waveform varies from  $\tau_w^* = 2.12 \times 10^{-7}$  to 1,368 % for e to Am respectively, note again that these values refer to the range of strain rates operating on atomic waveform envelopes within the vacuum. The corresponding values are:  $\tau_p^o = 3.49 \times 10^{15}$  to  $8.67 \times 10^{20}$  % for macrocosmic particulate forms, and  $\tau_r^* \cong \tau_p' = 1.74 \times 10^{15}$  to  $1.12 \times 10^{25}$  % for microcosmic particulate forms respectively; these incredible values decide radioactivity.

#### 3. Classical Mechanics Factors that Govern Radioactivity

Fig. 3 shows that values of the atomic waveform's centripetal force  $F_w$  (or  $F_p^*$ ), modulus  $\epsilon_w$ , and stress  $\sigma_w$  converge gradually with an increase in Z value and become similar within the range  $Z_R = 90$  to 99, i.e., elements Gd to Ta. In contrast, values of the same properties of the visible particulate atom diverge monotonously with an increase in Z value, Fig. 4. It is clear from the trends in Figs. 3 & 4 and Figs 5 & 6 that classical mechanics reveals that radioactivity results from changes in physical properties of the atom as Z value increases. Notably, the effect is a *microcosmic* phenomenon, the visible particulate atom plays no role whatsoever. The process involves the following three complementary mechanisms:

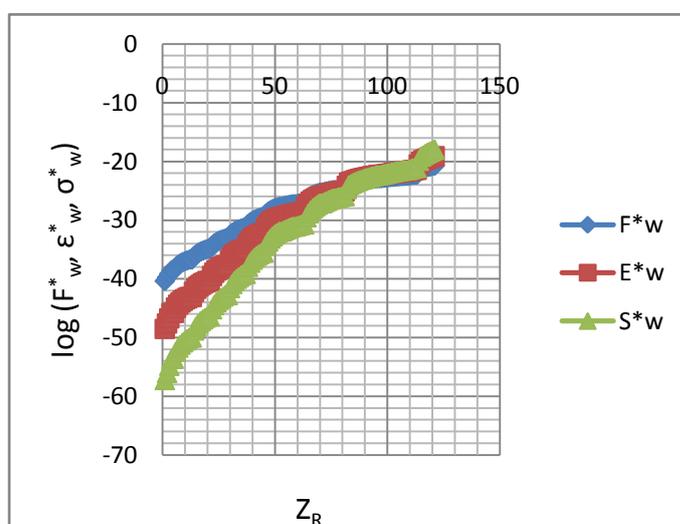


Fig. 3 Plot of  $\log(F_w, \epsilon_w$  and  $\sigma_w)$  vs. atomic no.  $Z_R$  – waveform

**(a) Convergence of absolute values of tensile properties of the microcosmic atom**

Values of physical properties of microcosmic forms of some heavy elements are listed in Table 3, the complete range is illustrated in Fig.3. As periodicity proceeds from e to Am, relative values of the waveform's tensile properties  $F_w$ ,  $\epsilon_w$ , and  $\sigma_w$  pass through a common point at Ac ( $Z_R = 115$ ) where the stress field  $\sigma_w$  is able to overcome the restraining effects of the stiffness  $\epsilon_w$  and centripetal force  $F_w$  holding the matrix together, here  $\sigma_w \cong 2\epsilon_w \cong 10F_w$ , the point, occurring at actinium Ac marks onset of spontaneous radioactivity.

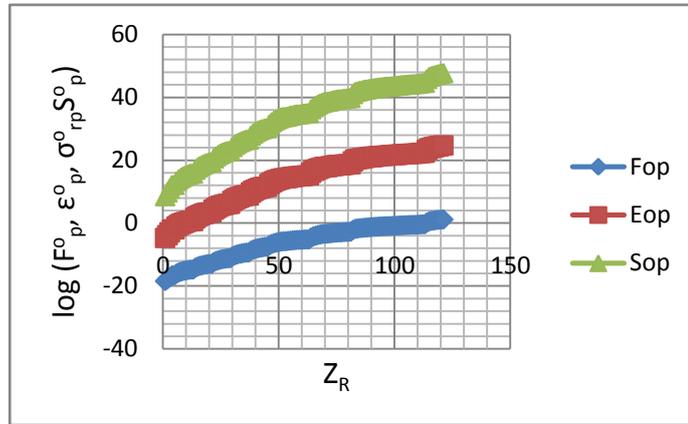


Fig. 4 Plot of  $\log(F_p, \epsilon_p \text{ and } \sigma_p)$  vs.  $Z_R$  –particulate form

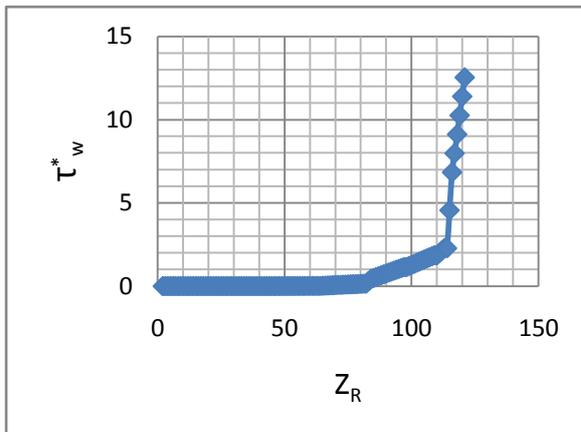


Fig. 5 Plot of  $\tau_w^*$  vs.  $Z_R$  – waveform

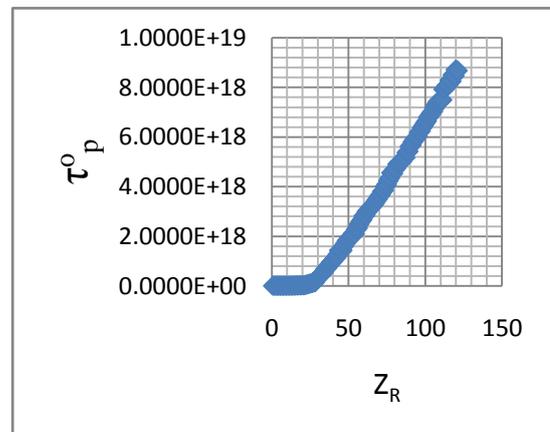


Fig. 6 Plot of  $\tau_p^0$  vs.  $Z_R$  – visible particulate form

**(b) Critical rate of strain on the atomic waveform**

Fig. 5 shows that values of  $\tau_w^*$  increase gradually from e's waveform value  $\tau_{w(e)}^* = 2.12 \times 10^{-7}$  to Xe ( $Z_R = 80$ )'s 143 % at which point it takes a sudden upward sweep and maintains the slope up to Ac ( $Z_R = 115$ ) where the value goes critical ( $\tau_{w(At)}^* = 214$  %, Table 3); this point (actinium) again marks onset of spontaneous radioactivity exactly as found for (a) above. We infer that at Ac strain rate on the local vacuum envelope (the “bosonic” waveform) encasing the particulate (“fermionic”) matter reaches an elastic limit; once ruptured, matrix particulate content slowly leaks into space in spontaneous radioactivity.

**(c) Critical value of angular speed of the atomic waveform**

Variation of strain  $\tau_w^*$  on the rotating waveform with angular speed  $\omega_w^*$  is illustrated in Fig. 7. From e's  $\omega_{w(e)}^* = 6.28$  rad/s the atomic waveform achieves an angular speed in excess of 6 billion rad/s precisely at Ac, see Table 3. The evidence would suggest that  $6 \times 10^9$  rad/s marks the critical value at which the rotating waveform acquires sufficient energy to engage the process of gradual attrition of its particulate content and eventual disintegration in spontaneous radioactivity.

If we assume the plum-pudding model, i.e., in the atomic nucleus particulate entities (fermions) are enclosed within corresponding waveforms (bosons) to form nuclides, radioactivity is explicable simply as a

process whereby the bosonic waveform is strained to a breaking point under severe centrifugal force of the spinning matrix; fermionic nuclides are thereby released in quanta sizes that depend among others on the element. Decay half-life is thus understood in the context of gradual release of some  $10^{20}$  strained molar pockets each containing  $6.623 \times 10^{43}$  units [6,7] at the rate of a few units per second in  $\alpha$ -,  $\beta$ -,  $\gamma$ -, or other decay.

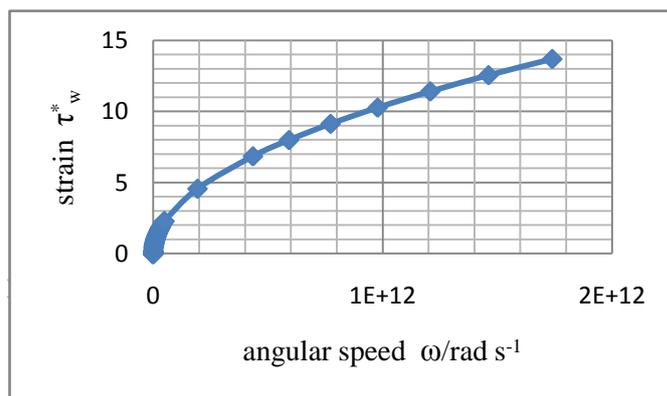


Fig. 7 Plot of strain  $\tau$  vs. angular speed  $\omega$

TABLE 3: Physical properties of some heavy elements' waveforms

Atom	Russ. At. No. $Z_R$	Atomic Radius, $r_w^*/m$	Volume, $v_w^*/m^3$	Density, $\rho_w^*/kg/m^3$	Angular Speed, $\omega_w^*/rads^{-1}$	Centripetal Force, $F_w^*/N$	Elastic Modulus $\epsilon_w^*/Pa$	Longtd. stress, $\sigma_w^*/Pa$	Strain rate, $\tau_w^*/\%$
Xe	80	2.234E+00	4.668E+01	1.060E-44	4.221E+08	1.965E-25	8.797E-26	1.254E-26	1.425E+1
Cs	81	2.234E+00	4.668E+01	1.060E-44	4.223E+08	1.965E-25	8.797E-26	1.254E-26	1.425E+1
Ba	82	1.117E+00	5.835E+00	1.696E-43	8.432E+08	7.859E-25	7.037E-25	2.006E-25	2.850E+1
La	83	7.445E-01	1.729E+00	8.585E-43	1.264E+09	1.768E-24	2.375E-24	1.015E-24	4.275E+1
Ce	84	6.599E-01	1.204E+00	1.391E-42	1.433E+09	2.251E-24	3.411E-24	1.645E-24	4.823E+1
Pm	87	4.922E-01	4.993E-01	4.497E-42	1.911E+09	4.047E-24	8.223E-24	5.318E-24	6.468E+1
Sm	88	4.537E-01	3.912E-01	6.226E-42	2.082E+09	4.762E-24	1.050E-23	7.364E-24	7.016E+1
Eu	89	4.208E-01	3.122E-01	8.412E-42	2.244E+09	5.535E-24	1.315E-23	9.949E-24	7.564E+1
Gd	90	3.924E-01	2.531E-01	1.113E-41	2.401E+09	6.367E-24	1.622E-23	1.316E-23	8.112E+1
Tb	91	3.676E-01	2.080E-01	1.445E-41	2.562E+09	7.256E-24	1.974E-23	1.710E-23	8.660E+1
Dy	92	3.457E-01	1.730E-01	1.848E-41	2.722E+09	8.203E-24	2.373E-23	2.185E-23	9.208E+1
Ho	93	3.263E-01	1.455E-01	2.328E-41	2.893E+09	9.209E-24	2.823E-23	2.754E-23	9.756E+1
Yb	96	2.792E-01	9.117E-02	4.342E-41	3.374E+09	1.258E-23	4.504E-23	5.135E-23	1.140E+2
Lu	97	2.792E-01	9.117E-02	4.342E-41	3.374E+09	1.258E-23	4.504E-23	5.135E-23	1.140E+2
Hf	98	2.642E-01	7.724E-02	5.415E-41	3.562E+09	1.404E-23	5.316E-23	6.405E-23	1.205E+2
Ta	99	2.507E-01	6.601E-02	6.677E-41	3.763E+09	1.560E-23	6.220E-23	7.897E-23	1.270E+2
W	100	2.385E-01	5.686E-02	8.148E-41	3.952E+09	1.723E-23	7.222E-23	9.637E-23	1.334E+2
Re	101	2.275E-01	4.932E-02	9.849E-41	4.141E+09	1.894E-23	8.325E-23	1.165E-22	1.399E+2
Os	102	2.174E-01	4.306E-02	1.180E-40	4.334E+09	2.073E-23	9.536E-23	1.396E-22	1.464E+2
Ir	103	2.082E-01	3.781E-02	1.404E-40	4.522E+09	2.261E-23	1.086E-22	1.660E-22	1.529E+2
Pt	104	1.998E-01	3.339E-02	1.657E-40	4.714E+09	2.457E-23	1.230E-22	1.960E-22	1.593E+2
Au	105	1.920E-01	2.963E-02	1.943E-40	4.911E+09	2.660E-23	1.386E-22	2.298E-22	1.658E+2
Hg	106	1.847E-01	2.641E-02	2.265E-40	5.103E+09	2.872E-23	1.555E-22	2.679E-22	1.723E+2
Tl	107	1.780E-01	2.364E-02	2.626E-40	5.292E+09	3.092E-23	1.737E-22	3.105E-22	1.788E+2

Pb	108	1.718E-01	2.125E-02	3.027E-40	5.482E+09	3.321E-23	1.933E-22	3.580E-22	1.853E+2
Bi	109	1.718E-01	2.125E-02	3.027E-40	5.482E+09	3.321E-23	1.933E-22	3.580E-22	1.853E+2
Po	110	1.595E-01	1.701E-02	4.072E-40	5.911E+09	3.851E-23	2.414E-22	4.816E-22	1.995E+2
At	111	1.489E-01	1.383E-02	5.366E-40	6.323E+09	4.421E-23	2.969E-22	6.346E-22	2.138E+2
Rn	112	1.396E-01	1.140E-02	6.946E-40	6.754E+09	5.030E-23	3.603E-22	8.215E-22	2.280E+2
Fr	113	1.396E-01	1.140E-02	6.946E-40	6.754E+09	5.030E-23	3.603E-22	8.215E-22	2.280E+2
Ra	114	6.980E-02	1.425E-03	1.111E-38	1.353E+10	2.012E-22	2.882E-21	1.314E-20	4.560E+2
Ac	115	4.653E-02	4.221E-04	5.627E-38	2.022E+10	4.527E-22	9.728E-21	6.655E-20	6.840E+2
Th	116	3.989E-02	2.658E-04	1.042E-37	2.364E+10	6.162E-22	1.545E-20	1.233E-19	7.980E+2
Pa	117	3.490E-02	1.781E-04	1.778E-37	2.702E+10	8.048E-22	2.306E-20	2.103E-19	9.121E+2
U	118	3.102E-02	1.251E-04	2.848E-37	3.044E+10	1.019E-21	3.283E-20	3.369E-19	1.026E+3
Np	119	2.792E-02	9.117E-05	4.341E-37	3.372E+10	1.257E-21	4.504E-20	5.135E-19	1.140E+3
Pu	120	2.538E-02	6.850E-05	6.356E-37	3.714E+10	1.522E-21	5.995E-20	7.518E-19	1.254E+3
Am	121	2.327E-02	5.276E-05	9.002E-37	4.054E+10	1.811E-21	7.783E-20	1.065E-18	1.368E+3

### SUMMARY AND CONCLUSION

The results are summarized.

1. Wave-particle duality is to be understood in the wider context that every atom comprises complementary wave and particulate forms mutually interactive but geometrically orthogonal, each form is characterized by its specific de Broglie quantum wavelength.
2. The microcosm comprises wave and invisible particulate matter while the macrocosm comprises wave embedded particulate matter only. Physical properties of the vacuum are therefore characterized not by single but a range of values of properties of the combined wave and microcosmic particulate forms. The combined waveforms manifest as vacuum radiation whose wavelengths make up the e-m spectrum.
3. The isolated particulate non-bonded atom, free from influence of a field other than its own, is possibly the densest object in the cosmos with microcosmic particulate Am topping the list at an incredible  $3.296 \times 10^{73} \text{ kg m}^{-3}$ . The microcosm thus consists of wave and particulate forms; the waveforms present as vacuum, its radiation (energy) gives rise to the CMB, while particulate forms present as *dark* matter and *dark* energy.
4. In contrast with the value of its radius in an external field, radius of the isolated atom decreases exponentially with an increase in  $Z$  value. Since literature values often refer to theoretical models or particulate (i.e., molar) matter, it is argued that effects of chemical environment such as bonding must be responsible for observed reverse trend.
5. In the context of SHM formalism light does not travel in the sense of rectilinear motion, it is an e-m harmonic oscillation; thus, cosmological distances are not distances of translation of the photon but accessible extent of electron waveform's cosmic permeation.
6. It is shown that the atom spins at incredible angular speeds,  $\omega$  values range from 6.3 to  $4.1 \times 10^{10} \text{ rad/s}$  for wave and 12.78 to  $4.12 \times 10^{10} \text{ rad/s}$  for particulate forms; notably, each form rotates independently indicative of significant degree of geometric freedom between the three universes or reference frames.
7. Three mechanisms involving changes in values of the atom's physical parameters are revealed to account for radioactivity; in each case spontaneous radioactive decay is shown to commence at actinium in line with observation.
8. The present account of the radioactive process fits with an atomic model that identifies the wave and particulate forms with bosons and fermions respectively.

We conclude that the investigation has produced compelling evidence to affirm validity of Russell's  $\vartheta$  values; their use facilitates classical (Newtonian) mechanics description of the atom. More significantly, SHM analyses using the  $\vartheta$  values have yielded theoretical results that reproduce empirical values with remarkable accuracy. Based on the present approach it should be possible to develop a consistent classical atomic physics to complement quantum mechanics.

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## APPENDIX: DEFINITIONS AND SAMPLE CALCULATIONS

### I. DEFINITIONS

#### 1. Forms and domains

Two forms: wave and particulate. Three mutually interactive but orthogonal domains: microcosmic Absolute Ref. Frame  $U_{abs}^*$  plus its Relative Component  $U_r^*$ ; macrocosmic Visible Ref. Frame  $U^o_r$ ; and microcosmic Invisible Analogue of the Visible Frame,  $U_r'$ .

#### 2. Absolute atomic mass

$$m_{abs}^* = m_w^* = h\vartheta_{abs}^*/c^2, \quad (A1)$$

where  $\vartheta_{abs}^*$  (i.e.,  $\vartheta_w^*$ ) is given (Russell's original field values [5,7]); h, Planck constant and c is speed of light in vacuum.

#### 3. Relative atomic mass

$$m_{p(E)}^i/g \text{ mol}^{-1} = (m_{abs(E)}^*/g \text{ atom}^{-1})/(m_{abs(H)}^*/g \text{ atom}^{-1}) \quad (A2)$$

where i, E, and H refer to domain, element, and hydrogen respectively.

#### 4. Field and corresponding mass values

Three field  $\vartheta$  values for each domain:  $\vartheta_w^*$ ,  $\vartheta_{p2}^*$ ;  $\vartheta_p^o$ ,  $\vartheta_{p1}^o$ ,  $\vartheta_{p2}^o$ ;  $\vartheta_p'$ ,  $\vartheta_{p1}'$ , and  $\vartheta_{p2}'$ ; subscript p1 refers to theoretical values, i.e., equilibrium conversion of the mole to constituent single atoms, see ref. [18];  $\vartheta_w^* = \vartheta_{p1}^* \cong \vartheta_{p1}'$  - they refer to microcosmic waveforms of  $U_{abs}^*$  and  $U_r'$ . The corresponding mass values are:  $m_{abs}^*$ ,  $m_{p1}^*$ ,  $m_{p2}^*$ ;  $m_p^o$ ,  $m_{p1}^o$ ,  $m_{p2}^o$ ;  $m_p'$ ,  $m_{p1}'$  and  $m_{p2}'$ . Generally,  $m_{p2}^* \cong m_{p2}'$ , therefore only  $U_r^*$  values are provided to illustrate trends of microcosmic particulate forms.

#### 5. Transverse radiation

For waveforms,  $c = 2.99792458 \times 10^8$  m/s; for particulate forms,  $c^* = c^o = c' = 3.71535229 \times 10^{-14}$  m/s obtained from “Einstein” plot, i.e.,  $\log(h\vartheta_{r1}^*)$  vs.  $\log(m_{p1}^*)$ , see ref. [5]; or calculated from the ratio  $(h\vartheta_{p1}^i/m_{p1}^i)^{1/2}$  where  $i$  denotes the particulate form’s domain, i.e.,  $U_r^*$ ;  $U_r^o$  or  $U_r'$ .

III. QUANTATIVE EXPRESSIONS

$$i. \quad m_{p1(E)}^*/g \text{ atom}^{-1} = m_{r(E)}^i/g \text{ mol}^{-1} * m_{abs(H)}^*/g \text{ atom}^{-1}, \tag{A3}$$

It converts molar mass g/mol to wave equiv. g/atom;  $m_{abs(H)}^*$  is domain invariant unit (i.e., H atom’s) molar mass [7].

$$ii. \quad \vartheta_{p1}^i = m_{p1}^*/m_{p(e)}^* = (m_{p1}^*/g \cdot \text{atom}^{-1}) / (7.372496678 \times 10^{-48} g / (\text{atom} \cdot \text{Hz})), \tag{A4}$$

where  $m_{p(e)}^* = (h\vartheta_{abs(e)}^*/c^2) / m_{abs(H)}^*$  and  $\vartheta_{abs(e)}^* = 1.0$  Hz [5],  $\vartheta_{p1}^i$  is not relevant here, it is presented for illustration only.

$$iii. \quad \vartheta_{p2}^i = m_p^* \times c_f^2 / h, \tag{A5}$$

where  $c_f$  refers to relevant transverse field, wave or particulate, i.e.,  $c = 2.99792458 \times 10^8$  for waveform or  $3.71535229 \times 10^{-14}$  m/s for particulate form.

III. SAMPLE EVALUATION PROCEDURE USING H

$$\begin{aligned} m_{abs(H)}^* &= h\vartheta_{abs(H)}^*/c^2 = 6.62606957 \times 10^{-27} \times 2048 / (2.99792458 \times 10^{10})^2 \\ &= 1.50988732 \times 10^{-44} g/\text{atom} - \text{microcosmic wave form.} \\ m_{p2(H)}^* &= [m_{abs(H)}^*/m_{abs(H)}^*] \times 10^{-3} = 1.0 \times 10^{-3} \text{ kg/mol} \\ \vartheta_{p2(H)}^* &= 1.0 \text{ kg/mol} \times (3.71535229 \times 10^{-12})^2 / (6.62606957 \times 10^{-27}) \\ &= 2083.262558 \text{ Hz} - \text{microcosmic particulate form} \\ \vartheta_{abs(H)}^* &= 2048 \text{ Hz} - \text{microcosmic wave form, given see refs. [5,7].} \\ m_{p2(H)}^* &= h\vartheta_{p2(H)}^*/c^{*2} \\ &= (6.62606957 \times 10^{-34} \times 2083.262558) / (3.71535229 \times 10^{-14})^2 \\ &= 1 \times 10^{-3} \text{ kg/mol} \\ m_{p2(H)}^o &= 2 \times m_{p2(H)}^* = 2 \times 10^{-3} \text{ kg/mol, visible molar form, see [5].} \\ \vartheta_{p2(H)}^o &= 2.0 g/mol \times (3.17535229 \times 10^{-12})^2 / (6.62606957 \times 10^{-27}) \\ &= 4166.525115 \text{ Hz} - \text{macrocosmic particulate form} \end{aligned}$$

Values so obtained for all elements were used in eqs. (1) - (7) to obtain values of atomic physical properties in Tables 1, 2 and 3; they are collated for H atom below in Table 4.

TABLE 4: H-atom's field and mass values for SHM analysis

	$\vartheta_{abs}^*$	$\vartheta_{r2}^*$	$\vartheta_{r2}^o$	$\vartheta_{r2}'$
		e-m field/Hz		
$U_{abs}^*$ (wave)	2048			
$U_r^*$ (particle)		2083.3		
$U_{r2}^o$ (particle)			4166.5	
$U_{r2}'$ (particle)				2083.3
		Molar mass u /kg atom <sup>-1</sup> or kg mol <sup>-1</sup>		
$U_{abs}^*$ (wave)	$1.51 \times 10^{-47}$			
$U_r^*$ (particle)		1		
$U_{r2}^o$ (particle)			2	
$U_{r2}'$ (particle)				1
Vacuum radiation $c = 2.99792458 \times 10^8$ m/s – waveform				
Molar radiation $c^* = c^o = c' = 3.71535229 \times 10^{-14}$ m/s – particulate form				