

# Implementation of Stronger S-Box for Advanced Encryption Standard

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## -----ABSTRACT-----

Advanced Encryption Standard (AES) block cipher system is widely used in cryptographic applications. The main core of AES block cipher is the substitution table or SBox. This S-box is used to provide confusion capability for AES. In addition, to strengthen the S-Box against algebraic attacks, the affine transformation is used. The requirements of information security within an organization have undergone several changes in the last few decades. With the fast evolution of digital data exchange, security of information becomes much important in data storage and transmission. The proposed paper presents a combinational logic based s-box implementation for subBbyte transformation in advanced encryption standard (AES) algorithm in verilog code language, this combinational logic based s-box is small area occupied and provide high throughput .this is a two staged pipelined combinational logic based s-box.the fact that pipelining can be applied to this S-Box implementation as compared to the typical ROM based lookup table implementation which access time is fixed and unbreakable. In this paper, the construction procedure for implementing a 2 stage pipeline combinational logic based network for the typical in a step-by-step manner. Finally, for the purpose of practicality, the depth of the mathematics involved has been reduced in order to allow the reader to better understand the internal operations within the S-Box. the simulation and synthesis is done in modelsim and Xilinx software ,output result has been included.

## **KEYWORDS:** sbox, encryption, sub byte

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# I. INTRODUCTION

Data Encryption Standard (DES) which was introduced in November 1976 when DES was no longer secure. On 2nd January 1997, the National Institute of Standards and Technology (NIST) invited proposals for new algorithms for the new Advanced Encryption Standard (AES). The goal was to replace the older after going through 2 rounds of evaluation; Rijndael was selected and named the Advanced Encryption Standard algorithm on 26<sup>th</sup> November 2001. The AES is a128bit input block with a key size of 128,198,256bits .the input 128 it(16 bytes) are swapped according to the predefined tables. These bytes are placed in

4x4 matrix. the elements in the matrix are rotated to the right in a line matrix. the rotation is varied with the line number the matrix undergo through a linear transformation which consist of the binary multiplication of each matrix elements with polynomial foam a auxiliary matrix, the  $GF(2^8)$  is used in the process of multiplication for better diffusion of bits the linear transformation is done over several times .finally the matrix are XOR with each other and the intermediate matrix is obtained these operations are repeated several times and define turn for 128,18,and 256 AES require respectively 10,12 or14 rounds. Mainly there are four transformations they are AddRoundKey,SubByte,ShiftRow and MixColum transformation.the add round key transformation is done by XOR operation between the state array and the output of the round key f key expansion function. the subbyte transformation is nonlinear byte substation of each byte in the state array a\is repeated with another one from a look up table called s-box, shift roe transformation is done y cyclically shifting the rows in the array with different offsets finally mix column transformation is done by mixing columns operation when the byte in the new column are obtained by the bytes of a coloum nth state array

**Previous Implementations of the S-Box :** In the previous implantation of the s-box further sub byte operation was done by using pre computed values stored in arm based lookup tables, here all the 256 values are stored in a rom which suffers from an unbreakable delay since ROMs have a fixed access time for its read and write operation. Furthermore this implantation is expensive in terms of hardware.

**Proposed implementation of s-box:** this is a more refined way of implementing the s-box is use of combinational logic .this s-box has the advantage of having small area occupancy in addition to be capable f being pipelined for increased performance in clock frequency. the s-box architecture is based on the combinational logic implementation

**The SubByte and InvSubByte Transformation:** The SubByte transformation is done by taking the multiplicative inverse in  $GF(2^8)$  then by an affine transformation. For its reverse, the InvSubByte transformation, the inverse affine transformation is obtained to the get multiplicative inverse. The steps involved for both transformation is shown below.

SubByte: 1 Multiplicative Inversion in GF(28) 2. Affine Transformation

InvSubByte:3Inverse Affine Transformation 4 Multiplicative Inversion in GF(28)

The Affine Transformation and its inverse can be represented in matrix form and it is shown below.

The AT and AT-1 are the Affine Transformation and its inverse Affine Transformation while the vector *a* is the multiplicative inverse of the input byte from the state array. Both the SubByte and the InvSubByte transformation involve a multiplicative inversion operation. Thus, both transformations may actually share the same multiplicative inversion module in a combined architecture. An example of such hardware architecture is shown below. Switching between SubByte and InvSubByte is just a matter of changing the value of INV. INV is set to 0 for SubByte while 1 is set when InvSubByte operation is desired.



#### II. S-BOX CONSTRUCTION METHODOLOGY

The procedure for constructing the multiplicative inverse module for the s-box using composite field arithmetic . it is stated that any arbitrary polynomial can be represented as bx + c, given an irreducible polynomial of  $x^2 + Ax + B$ . Thus, element in GF(28) may be represented as bx + c where b is the most significant nibble while c is the least significant nibble. From here, the multiplicative inverse can be computed

using the equation below. [2]

$$(bx + c)^{-1} = b(b^2B + bcA + c^2)^{-1}x + (c + bA)(b^2B + bcA + c^2)^{-1}$$

From [1], the irreducible polynomial that was selected was  $x^2 + x + \lambda$ . Since A = I and  $B = \lambda$ , then the equation could be simplified to the form as shown below. [1]

$$(bx+c)^{-1} = b(b^{2}\lambda + c(b+c))^{-1}x + (c+b)(b^{2}\lambda + c(b+c))^{-1}$$

The above equation indicates that there are multiply, addition, squaring and multiplication inversion in GF(24) operations in Galois Field. Each of these operators can be transformed into individual blocks when constructing the circuit for computing the multiplicative inverse. From this simplified equation, the multiplicative inverse circuit  $GF(2^8)$  can be produced as

shown in Figure 2.1



Figure 2.1. Multiplicative inversion module for the S-Box. [1]

The legends for the blocks within the multiplicative inversion module from above are illustrated in the Figure 2.2 below



Figure 2.2. Legends for the building blocks within the multiplicative inversion module.

**Isomorphic Mapping and Inverse Isomorphic Mapping:** The multiplicative inverse calculation has been done by decomposing the more complex GF(28) to lower order fields of

GF(2<sup>2</sup>) -> GF(2) :  $x^2 + x + 1$ GF((2<sup>2</sup>)<sup>2</sup>) -> GF(2<sup>2</sup>) :  $x^2 + x + \varphi$  (2.3) GF(((2<sup>2</sup>)<sup>2</sup>)<sup>2</sup>) -> GF((2<sup>2</sup>)<sup>2</sup>) :  $x^2 + x + \lambda$ where  $\varphi = \{10\}2$  and  $\lambda = \{1100\}2$ .

Multiplicative inverse in composite fields cannot be directly applied to an element which is based on  $GF(2^8)$  by using isomorphic function the elements has t be mapped into composite fields represented and obtained the multiplicative inverse .the result has to again mapped into composite fields to equivalent into gf(28) by using inverse isomorphic function

	(1	0	1	0	0	0	0	0)	(97)		(1	1	1	0	0	0	1	0	(	97
	1	1	0	1	1	1	1	0	$q_{6}$		0	1	0	0	0	1	0	0		$q_{6}$
	1	0	1	0	1	1	0	0	$q_5$		0	1	1	0	0	0	1	0		$q_5$
Sva-	1	0	1	0	1	1	1	0	$q_4$	5-1	0	1	1	1	0	1	1	0		$q_4$
$o \times q =$	1	1	0	0	0	1	1	0	$q_3$	$o \times q =$	0	0	1	1	1	1	1	0	~	$q_3$
	1	0	0	1	1	1	1	0	$q_2$		1	0	0	1	1	1	1	0		$q_2$
	0	1	0	1	0	0	1	0	$q_1$		0	0	1	1	0	0	0	0		$q_1$
	0	1	0	0	0	0	1	1)	q0)		0	1	1	1	0	1	0	1)		90

**Composite Field Arithmetic Operations :** An arbitrary polynomial operation can be represented by bx+c whee b is the upper half term and the c is the lower half term for instance arbinary number I galis field can be spit to qhx+ql, if  $q = \{1011\}2$ , it can be represented as  $\{10\}2x + \{11\}2$ , where qH is  $\{10\}2$  and  $qL = \{11\}2$ . qH and qL can be further decomposed to  $\{1\}2x + \{0\}2$  and  $\{1\}2x + \{1\}2$  respectively. Then the decomposing is done by making using f irreducible polynomial using this idea the logical equitation for the addition, squaring, multiplication and inversion can be derived.

Addition in  $GF(2^4)$ : Addition of 2 elements in Galois Field can be translated to simple bitwise XOR operation between the 2 elements.

Squaring in GF(2<sup>4</sup>): Let k = q2, where k and q is an element in GF(24), represented by the binary number of  $\{k3 \ k2 \ k1 \ k0\}^2$  and  $\{q3 \ q2 \ q1 \ q0\}^2$  respectively.

$$\begin{split} k &= \left( \underbrace{k_{3}k_{2}}_{k_{H}} \underbrace{k_{1}k_{0}}_{k_{L}} \right) = k_{H}x + k_{L} = \left( \underbrace{q_{3}q_{2}}_{q_{H}} \underbrace{q_{1}q_{0}}_{q_{L}} \right)^{2} = \left( q_{H}x + q_{L} \right)^{2} \\ k &= q_{H}^{2}x^{2} + q_{H}q_{L}x + q_{H}q_{L}x + q_{L}^{2} = q_{H}^{2}x^{2} + q_{L}^{2} \end{split}$$

The *x*<sup>2</sup> term can be modulo reduced using the irreducible polynomial from (2.3),  $x^2 + x + \varphi$ . By setting  $x^2 = x + \varphi$  and replacing it into x2. Doing so yields the new expressions below.

$$k = q_{H}^{2}(x + \varphi) + q_{L}^{2}$$
  

$$k = \underbrace{q_{H}^{2}}_{k_{T}} x + \underbrace{(q_{H}^{2}\varphi + q_{L}^{2})}_{k_{T}} \in GF(2^{2})$$

The expression above is now decomposed to  $GF(2^2)$ . Decomposing *kH* and *kL* further to GF(2) would yield the formula to compute squaring operation in  $GF(2^2)$ . Using the irreducible polynomial from (2.3)  $x^2 + x + 1$ , and setting it to  $x^2 = x + 1$ ,  $x^2$ 

is substituted and the new expression is obtained.

$$k_{H} = q_{3}(x+1) + q_{2}$$
  

$$k_{3}x + k_{2} = q_{3}x + (q_{2} + q_{3}) \in GF(2)$$

$$\begin{split} k_{L} &= q_{3}(1) + q_{2}x + q_{1}(x+1) + q_{0} \\ k_{1}x + k_{0} &= (q_{2} + q_{1})x + (q_{3} + q_{1} + q_{0}) \in GF(2) \end{split}$$

From equations (2.4) and (2.5), the formula for computing the squaring operation in GF(24) is acquired as shown below.

 $k_{3} = q_{3}$   $k_{2} = q_{3} \oplus q_{2}$   $k_{1} = q_{2} \oplus q_{1}$   $k_{0} = q_{3} \oplus q_{1} \oplus q_{0}$  (2.6)

Equation (2.6) can then be mapped to its hardware logic diagram and it is shown in Figure 2.3 below.



**Multiplication with constant,**  $\Box$ Let  $k = q\lambda$ , where  $k = \{k3 \ k2 \ k1 \ k0\}2$ ,  $q = \{q3 \ q2 \ q1 \ q0\}2$  and  $\lambda = \{1100\}2$  are elements of  $GF(2^{4}).$ 

$$k = \left(\underbrace{k_3 k_2}_{k_H} \underbrace{k_1 k_0}_{k_L}\right) = k_H x + k_L = \left(\underbrace{q_3 q_2}_{q_H} \underbrace{q_1 q_0}_{q_L}\right) \left(\underbrace{1100}_{\lambda_H} \underbrace{\lambda_L}\right)$$
$$k = \left(q_H x + q_L\right) (\lambda_H x + \lambda_L) \quad \lambda_L \text{ can be cancelled out since } \lambda_L = \{00\}_2.$$
$$k = q_H \lambda_H x^2 + q_L \lambda_H x$$

Modulo reduction can be performed by substituting  $x2 = x + \phi$  using the irreducible

polynomial in (2.3) to yield the expression below

$$k = q_H \lambda_H (x + \varphi) + q_L \lambda_H x$$

$$k = \underbrace{(q_H \lambda_H + q_L \lambda_H)}_{k..} x + \underbrace{(q_H \lambda_H \varphi)}_{k.} \in GF(2^2)$$

$$k_3 = q_2 \oplus q_0$$

$$k_2 = q_3 \oplus q_2 \oplus q_1 \oplus q_0$$

$$k_1 = q_3$$

$$k_0 = q_2$$

#### 2.2.4. GF(2<sup>4</sup>) Multiplication

Let k = qw, where  $k = \{k3 \ k2 \ k1 \ k0\}2$ ,  $q = \{q3 \ q2 \ q1 \ q0\}2$  and  $w = \{w3 \ w2 \ w1 \ w0\}2$  are elements of GF(24).

$$\begin{split} & k = \left(\underbrace{k_3 k_2 k_1 k_0}_{k_H - k_L}\right) = k_H x + k_L = \left(\underbrace{q_3 q_2 q_1 q_0}_{q_H - q_L}\right) \left(\underbrace{w_3 w_2 w_1 w_0}_{w_H - w_L}\right) = \left(q_H x + q_L\right) \left(w_H x + w_L\right) \\ & k = \left(q_H w_H\right) x^2 + \left(q_H w_L + q_L w_H\right) x + q_L w_L \end{split}$$

Substituting the x2 term with  $x^2 = x + \varphi$  yields the following.

$$k = (q_H w_H)(x + \phi) + (q_H w_L + q_L w_H)x + q_L w_L$$

$$k = k_H x + k_L = (q_H w_H + q_H w_L + q_L w_H)x + q_H w_H \phi + q_L w_L \in GF(2^2)$$
(2.10)

Equation (2.10) is in the form  $GF(2^2)$ . It can be observed that there exists addition and

multiplication operations in GF(22). As mentioned in Section 2.2.1, addition in GF(2<sup>2</sup>) is but bitwise XOR operation. Multiplication in GF(22), on the other hand, requires decomposition to GF(2) to be implemented in hardware. Also, it the expression would be too complex if equation (2.10) were to be broken down to GF(2). Thus, the formula for multiplication in GF(2<sup>2</sup>) and constant  $\varphi$  will be derived instead. Figure 2.5 below shows the hardware implementation for multiplication in GF(2<sup>4</sup>).



	0	1	2	3	4	5	6	7	8	9	a	b	с	d	e	f
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	1	2	3	4	5	6	7	8	9	a	b	с	d	e	f
2	0	2	3	1	8	a	b	9	с	e	f	d	4	6	7	5
3	0	3	1	2	с	f	d	e	4	7	5	6	8	b	9	a
4	0	4	8	с	6	2	e	a	b	f	3	7	d	9	5	1
5	0	5	a	f	2	7	8	d	3	6	9	с	1	4	b	e
6	0	6	b	d	e	8	5	3	7	1	с	a	9	f	2	4
7	0	7	9	e	a	d	3	4	f	8	6	1	5	2	с	b
8	0	8	с	4	b	3	7	f	d	5	1	9	6	e	a	2
9	0	9	e	7	f	6	1	8	5	с	b	2	a	3	4	d
a	0	а	f	5	3	9	с	6	1	b	e	4	2	8	d	7
b	0	b	d	6	7	с	a	1	9	2	4	f	e	5	3	8
с	0	с	4	8	d	1	9	5	6	a	2	e	b	7	f	3
d	0	d	6	b	9	4	f	2	e	3	8	5	7	a	1	с
e	0	e	7	9	5	b	2	с	a	4	d	3	f	1	8	6
f	0	f	5	a	1	e	4	b	2	d	7	8	3	с	6	9

The pre-computed multiplication result of 2 elements in GF(24) is tabled below.

From Table 2.1, the results for multiplication with constant  $\lambda$  and squaring operation in GF(24) can also be obtained

## **GF(2<sub>2</sub>) Multiplication**

Let k = qw, where  $k = \{k1 \ k0\}2$ ,  $q = \{q1 \ q0\}2$  and  $w = \{w1 \ w0\}2$  are elements of GF(2<sup>2</sup>).

$$k = (k_1 k_0) = k_1 x + k_0 = (q_1 q_0) (w_1 w_0) = (q_1 x + q_0) (w_1 x + w_0)$$
  

$$k = q_1 w_1 x^2 + q_0 w_1 x + q_1 w_0 x + q_0 w_0$$

The x2 term can be substituted with  $x^2 = x + 1$  to yield the new expression below.

$$\begin{aligned} & k = q_1 w_1 (x+1) + q_0 w_1 x + q_1 w_0 x + q_0 w_0 \\ & k_1 x + k_0 = (q_1 w_1 + q_0 w_1 + q_1 w_0) x + (q_1 w_1 + q_0 w_0) \in GF(2) \end{aligned}$$

Figure 2.6 below illustrates its hardware implementation



The hardware implementation above differs from the (2.12) for the computation of k1. It can be proven that the implementation above for computing k1, would result to the Expression in (2.12), as shown below

**Multiplication with constant**  $\Box$ Let  $k = q\varphi$ , where  $k = \{k1 \ k0\}2$ ,  $q = \{q1 \ q0\}2$  and  $\varphi = \{10\}2$  are elements of GF(22).

$$k = k_1 x + k_0 = (q_1 q_0)(10_2) = (q_1 x + q_0)(x)$$
  
$$k = q_1 x^2 + q_0 x$$

Substitute the *x*2 term with  $x^2 = x + 1$ , yield the expression below

$$k = q_1(x+1) + q_0 x$$
  

$$k = (q_1 + q_0)x + (q_1) \in GF(2)$$
(2.13)

From (2.13), the formula for computing multiplication with  $\varphi$  can be derived and is shown below.

$$k_1 = q_1 \oplus q_0$$
$$k_0 = q_1$$

The hardware implementation of multiplication with  $\phi$  is shown below in Figure 2.7



## Multiplicative Inversion in GF(24)

The authors of [3] has derived a formula to compute the multiplicative inverse of q (where q is an element of GF(24)) such that  $q-1 = \{q3-1,q2-1,q1-1,q0-1\}$ . The inverses of the individual bits can be computed from the equation below. [3]

## **III. SIMULATION RESULT:**

the above said implementation of the multiplicative inverse by using subbyte transformation in composite field has simulated in the modelsim software here the we can observe that the encryption has done by using the multiplicative inverse there are the fig of encryption and decryption of aes



Fig(1): encryption of the plain text by using the inverse multiplication module based s-box



Fig(2): decryption of the plain text by using the inverse multiplication module based s-box

# Synthesis report:





Device Utilization Summary								
Logic Utilization	Used	Available	Utilization	Note(s)				
Number of Slice Flip Flops	1,747	66,560	2%	-				
Number of 4 input LUTs	6,272	66,560	9%					
Number of occupied Slices	3,572	33,280	10%					
Number of Slices containing only related logic	3,572	3,572	100%					
Number of Slices containing unrelated logic	0	3,572	0%					
Total Number of 4 input LUTs	6,332	66,560	9%					
Number used as logic	6,272							
Number used as a route-thru	60							
Number of bonded <u>IOBs</u>	390	633	61%					
Number of BUFGMUXs	1	8	12%					
Average Fanout of Non-Clock Nets	4.38							

# fig: aes encryption block with device utilization summary

Device Utilization Summary							
Logic Utilization	Used	Available	Utilization	Note(s)			
Number of Slice Flip Flops	1,789	66,560	2%				
Number of 4 input LUTs	6,880	66,560	10%				
Number of occupied Slices	3,925	33,280	11%	ř.			
Number of Slices containing only related logic	3,925	3,925	100%				
Number of Slices containing unrelated logic	0	3,925	0%				
Total Number of 4 input LUTs	6,966	66,560	10%				
Number used as logic	6,880						
Number used as a route-thru	86						
Number of bonded <u>IOBs</u>	12	633	1%				
Number of BUFGMUXs	1	8	12%				
Average Fanout of Non-Clock Nets	4.33						

Fig aes decryption block with device utilization summary

# **IV. CONCLUSION:**

A combinational logic based S-Box for the SubByte transformation is discussed and its internal operations are explained. As compared to the typical ROM based lookup table, the presented implementation is both capable of higher speeds since it can be pipelined and small in terms of area occupancy This compact and high speed architecture allows the S-Box to be used in both area- limited and demanding throughput AES chips for various applications, ranging from small smart cards to high speed servers. The implementation of the stronger sbox by using inverse multiplication has done and the output result of simulation has show by using model simsoftware and synthsis is doneby using silinx softaware

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